

Comparing Free-Throw Forms Among NBA Players Through 3D Similarity Measures

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Abstract

In this paper, we propose a method to compare free-throw forms of various NBA players. Using publicly available SportVU tracking data from the 2015-16 NBA season [1], we identify instances of free-throw attempts and track the ball's motion while it's in the player's hands in order to isolate the given player's shot form from the data. To characterize each player's form, we apply a multivariate kernel density estimation to the sample of the player's free throw attempts. Furthermore, using a k-means clustering, we attempt to categorize the multivariate kernel density estimates across the sample of players, characterizing each cluster by the cluster mean. We then proceed to apply a variety of three-dimensional similarity measures to the clustered kernel density estimates, therein providing a variety of metrics by which we can assess free-throw form similarity among NBA players.

1 Introduction

With wider adoption of the principles taught by “Moreyball” [2], the average amount of three-point attempts per 100 possessions has dramatically risen over the course of the last decade in the NBA [3]. Accordingly, shooting is an increasingly important skill in NBA basketball, and of course, crucial to shooting success is player shooting form.

However, up to this point, player shooting form has predominantly existed as a qualitative study. Most attempts at any empiricism have been primitive, confined to countable measures such as release time, largely due to the unavailability of reliable, public data. Thus, we propose methods through which to isolate a player’s shot form from given tracking data, and furthermore propose viable methods through which multiple player’s three-dimensional shooting forms can be quantitatively compared.

2 Data Processing

In our analysis, we use publicly available SportVU tracking data from the 2015-16 NBA season [1]. Over the course of a basketball game, a player’s shooting form is evident in two distinct situations: jump shots in the midst of gameplay, and free-throw attempts.

2.1 Confounding Variables

There are two principle, quantifiable confounding variables in the relationship between the independent shooting form shape and a make/miss outcome: time and distance. Evaluating the former, in jump shots over the course of a game, a player’s shooting technique is influenced by the time left on the game clock, time left on the shot clock, and most significantly, the time they have to release the ball before it is blocked by an opposing player. Thus, at game instances where time is running, a player’s shooting form and their likelihood of a successful field goal attempt is invariably influenced and altered due to the confounding variable of time. In discussion of the latter confounder, distance, it is plausible that as distance to the basket varies, a player’s shooting form likewise varies to some degree in order to accommodate this change.

2.2 Data Selection

Thus, in an attempt to standardize situation and eliminate probable confounding variables, we have limited our analysis to player free-throw attempts. Because free-throws are attempted at a fixed distance and time is removed as an influencing constraint, they serve as a medium for functional isolation of a player’s shooting form in a purely spatial sense, thus making precise inter-player form comparison feasible. Because of the limited nature of the dataset, we set a low minimum of at least 10 observed free-throw attempts in the available sample of games in order for a player to qualify as a viable subject in the study.

2.3 Data Filtering

Using the SportVU tracking data in conjunction with Basketball Reference play-by-play logs, we can align the two datasets by game clock in order to isolate both instances of free-throw attempts and to ascertain the identity of the attempt-taker. Filtering for the actual shooting form, we look to capture the player's motion which affects the velocity and angle at which the ball is released, and get rid of all superfluous build up so as to isolate the "crux" of the shooting form for our comparative analysis. Because SportVU player tracking attempts to track the central position of a player at any given moment, the player's coordinates in the course of a free-throw attempt remain relatively sedentary. However, the ball's center is in motion, and the trajectory of the ball parallels the player's shooting motion, and thus we can use the ball's motion as a proxy for the player's holistic shooting form. We define the start of the shooting motion at the point where the ball's z-coordinate is higher than half of the player's height¹ and has continually moved up for at least 5 frames (1/5th of a second). We define the end of the shooting motion, the release, at the point where the ball's x and z-coordinates have exhibited parabolic motion for at least 5 frames².

2.4 Standardizing the Data

In order to agglomerate individual player free-throw attempt forms into a composite form and furthermore compare composite forms between players, we first must standardize the data. We first establish our coordinate system at a (0,0,0) origin located in the middle of the free-throw line, where moving towards the basket would be reflected by a negative x-coordinate, motion to the left and right parallel to the free-throw line would be reflected by negative and positive y-coordinates, respectively, and any upward motion would be reflected by an increasingly positive z-coordinate, dubbed in this analysis as the "radius" variable. We then can easily correct for free-throw attempts at different baskets, establishing the near basket as the paradigm and simply multiplying the (x,y) coordinates of attempts on the other basket by -1 in order to correct for direction. Additionally, because we want to isolate the shot form shape independent of handedness, we have to correct for varying dominant hands among players leading to directional differences in shot forms. Thus, assuming a dominant right hand, we define a prototypical shot form as temporally progressing from right to left, and thus invert the y-coordinates of all shot forms moving left to right.

¹ Player height data from NBA.com Player Bio data [4]

² Because SportVU data is prone to mechanical noise, we measure signal noise in each arena's tracking device by observing a sample of shots, after the point of release and before the ball had touched the rim, in each arena and measured the average residual between each recorded point and the best parabolic fit. This residual average was considered the degree of mechanical noise in each arena. If the residuals between 5 consecutive points and the best parabolic fit are within the given arena's residual average, it is defined as release.

2.5 Modeling the Data

To afford the maximum possible approaches of spatial comparison, we modeled each player's shooting form with two methods: trivariate local regression (LOESS) and three-dimensional kernel density estimation (KDE)³. An example is shown below in Figure 1^{4 5}.

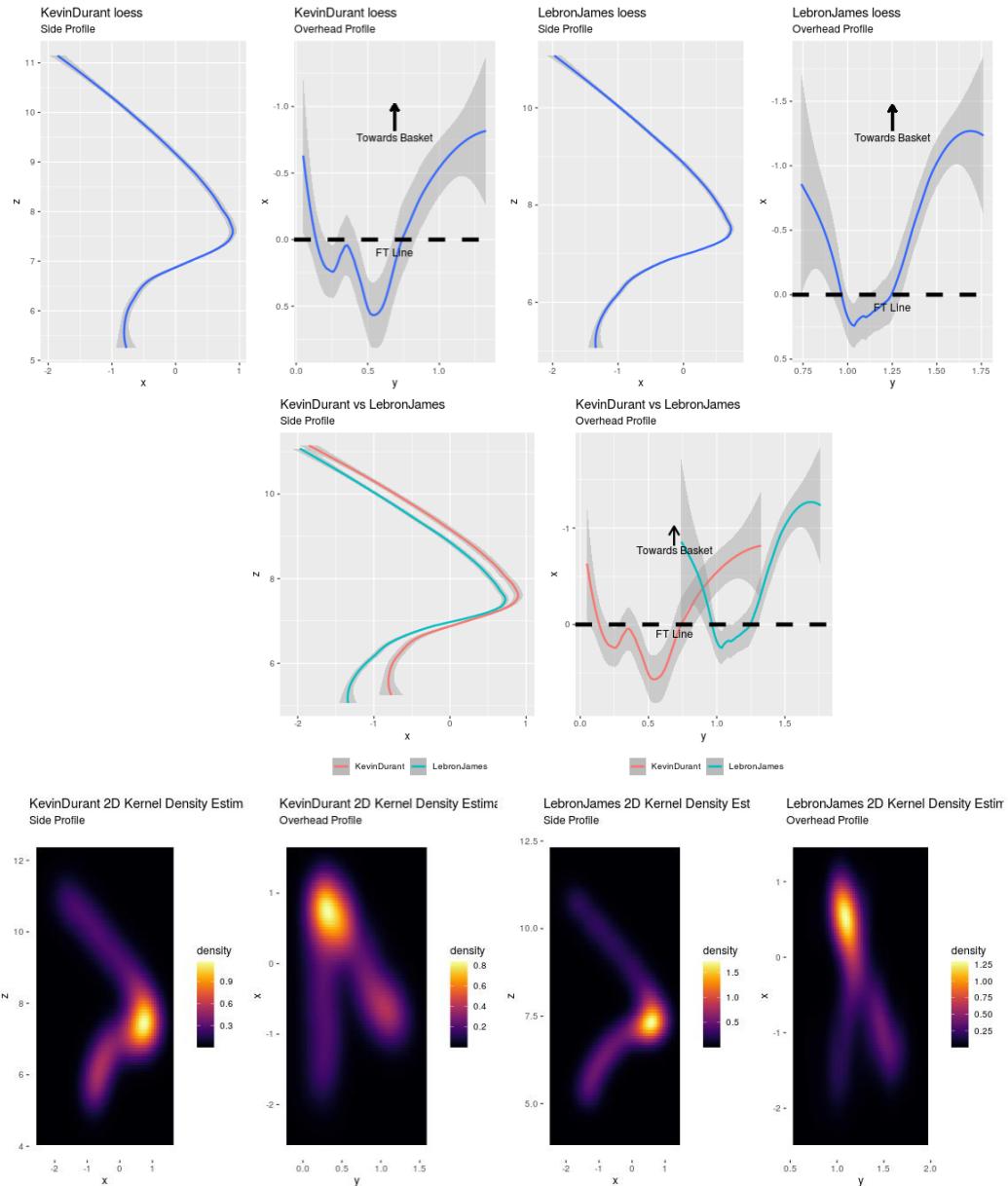


Figure 1: LOESS and KDE Comparative Representations

³ In order to enable comparison across players, we had to standardize a domain across which to calculate the three-dimensional kernel density estimate. We found that an x domain of (-2,1.75), a y domain of (-2,2), and a radius domain of (4,10.25) encapsulated >99% of all observed points across different player shot forms. We returned matrices of dimensions 300x320x500 from our kernel density estimates.

⁴ Density values reflected in Figure 1 are not the actual probability density values, but rather were significantly scaled up for ease of interpretability.

⁵ Plots are shown in two-dimensions with two-dimensional models for the sake of clear visualization.

3 Three-Dimensional Methods of Comparison

There are a number of popularized methods for comparing trajectories in three-dimensions. However, for our purposes, we need non-discretized methods of measuring three-dimensional similarity. Thus, in this paper, we will focus on three principal methods to assess dissimilarity: Frechet Distance, Euclidean Distance Matrices, and Kullback-Leibler Divergence.

3.1 LOESS Curve Frechet Distance

Because SportVU data is collected at constant time intervals, and because given players' shot forms vary in speed, between two players there doesn't exist an absolute frame of reference if we want to purely compare the actual shot form disregarding time. Thus, to overcome this obstacle, we can use the LOESS model we constructed in section 2.5. Systemically sampling 500 points from each player's LOESS fit⁶, we can use the Frechet Distance algorithm to map each point to its approximate corresponding point on the other player's form curve and calculate a similarity measure between the two player's curves [5]. The most significant drawback of this method is that because it can only be accomplished by modeling each player's shot form as a consolidated LOESS curve, the similarity measure functionally compares the mean of each player's shot form rather than accounting for potential variance and inconsistencies across the sample of each player's shot forms.

3.2 Bin Difference

Loosely paralleling the methodology outlined in section 3.1, to estimate the difference between two player's shot forms, we can simply calculate the bin difference between two three-dimensional arrays [6]. Using the 3D KDE model established in section 2.5, we can find the absolute difference in density estimate per corresponding cell between the two players' KDE arrays, and sum these absolute differences together to represent a holistic similarity measure.

3.3 Kullback-Leibler Divergence

The final, most robust method we use to estimate shot form similarity is calculating the three-dimensional Kullback-Leibler Divergence (KLD) between two player's shot forms. Kullback-Leibler Divergence is a method through which one can assess the similarity between two probability distributions [7]. The formula to calculate a three-dimensional Kullback-Leibler Divergence is given below in Formula 1:

$$KL(p, q) = \iiint_{-\infty}^{\infty} p(t) \log \left(\frac{p(t)}{q(t)} \right) dt$$

Where $t = (x, y, z)$, $dt = (dx, dy, dz)$, $p(t)$ represents the target probability distribution and $q(t)$ represents the competing probability distribution

Our 3D KDE model constructed in section 2.5 is a three-dimensional probability density function that integrates to 1; thus, we can substitute our determined three-dimensional kernel density estimates for two given players in lieu of probability distributions $p(t)$ and $q(t)$ while maintaining the integrity of the Kullback-Leibler Divergence.

Player 1	Player 2	3D Frechet Distance	3D Bin Difference	3D Kullbach-Leibler Divergence
KevinDurant	LebronJames	0.3635093	1.128533	1.480394

Table 1: Comparative Table of Kevin Durant and Lebron James⁷

Using our collected sample of players, we can deduce the correlogram below, showing the distribution and correlation between our various similarity measures and free-throw percentage.

Similarity Measures Correlogram

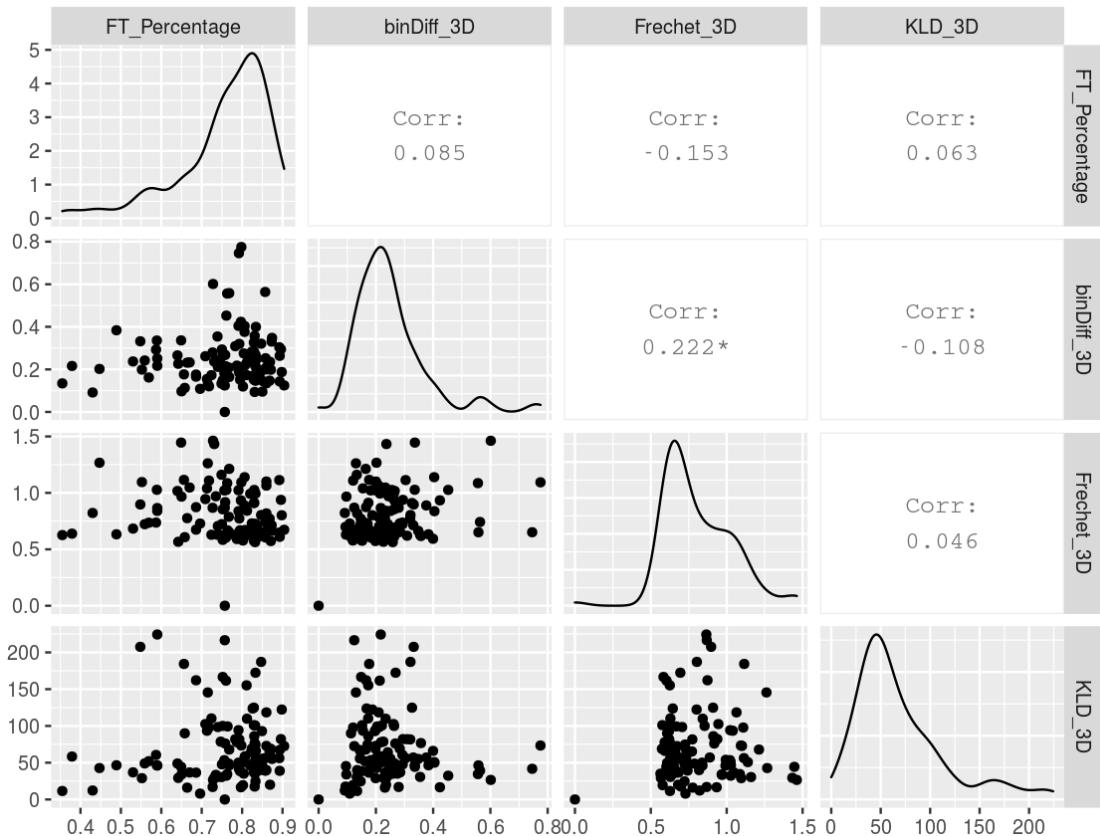


Figure 2: Similarity Measures Correlogram⁸

⁷ Player 1 Treated as Target Distribution

⁸ In Bin Difference and LOESS Distance calculations, composite average of all player shooting forms was treated as the base form for comparison. In Kullback-Leibler Divergence calculations, composite average of all player shooting forms is treated as the target probability distribution.

4 Clustering Shot Forms

In order to conduct a more generalized analysis on player shot forms, we can sort them into clusters using the k-means clustering algorithm. Using the elbow method, we identify that the sum of squares is minimized for our sample of players at 7 clusters. Thus, arranging our sample of player shot forms into 7 clusters, we can further characterize each cluster by the cluster mean, resulting in the following shot forms:

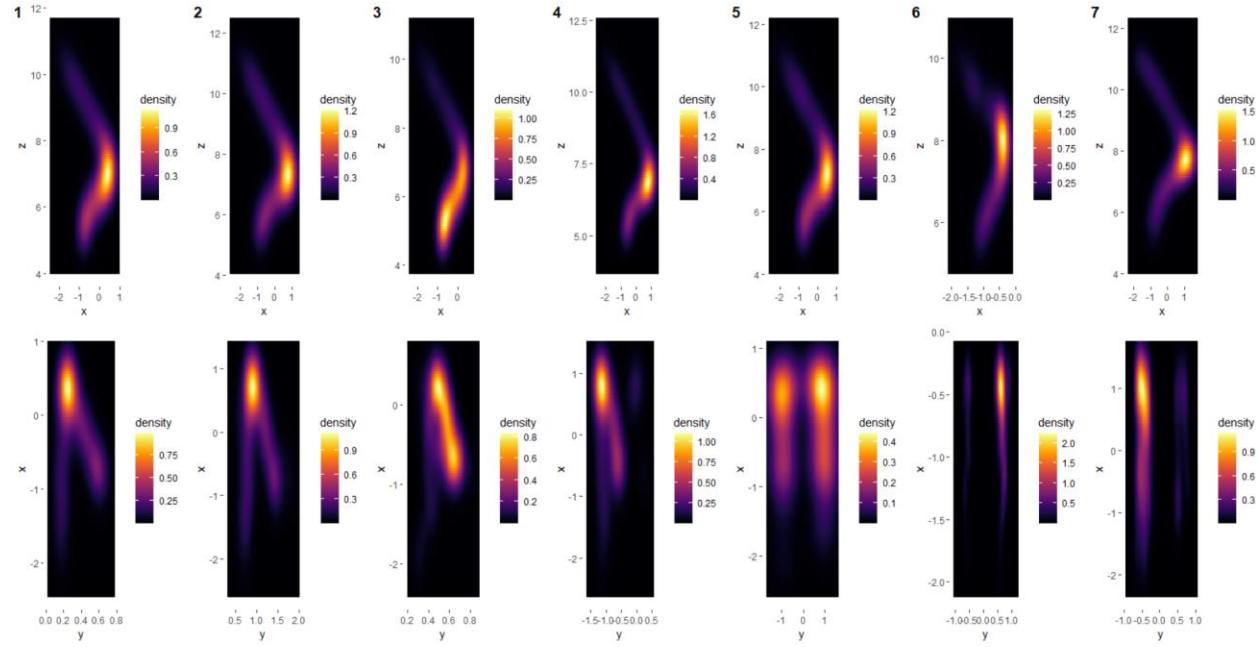


Figure 3: Clustered Shot Forms from Side and Overhead Vantage

Repeating the methodology outlined in section 3, we compare each cluster to the composite average of all player shooting forms with each of the outlined similarity measures⁹.

Table 2: Cluster Comparative Table⁷

Cluster	FT%	3D Frechet Distance	3D Bin Difference	3D Kullbach-Leibler Divergence
1	0.593	0.52732	1.67749	10.17620
2	0.685	0.89270	1.58114	7.41660
3	0.779	0.63914	1.60710	4.67237
4	0.548	0.74580	1.74398	9.94691
5	0.752	0.48673	1.79881	12.38330
6	0.682	0.66081	1.92376	17.48540
7	0.764	0.53964	1.83774	14.67780

5 Conclusion

Throughout this paper, we have proposed methods to compare free-throw forms of various NBA players, both individually and generalized within clusters. We have outlined viable methods of producing three-dimensional similarity measures, calculating inter-player/cluster three-dimensional Frechet Distance, three-dimensional Bin Difference, and three-dimensional Kullback-Leibler Divergences.

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