Statistical Computing (36-350)
Lecture 1: Introduction to the course; Data

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Why good statisticians learn how to program

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HONESTY: otherwise, you end up distorting the problem to match the tools you happen to have
CLARITY: turning your method into something a machine can do forces you to discipline your thinking and make it communicable; and science is public
How this class will work

First half: general programming, with statistical illustrations
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Second half: computational tasks especially relevant to statistics, using general programming ideas
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∴ *Keep up with the readings and exercises*
Two lectures a week on concepts and methods
Lab to try out stuff and get immediate feedback
HW to do longer and more complicated things
Exam to check understanding
Project to show actual competence
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*Keep up with the readings and exercises*
Assignments, office hours, class notes, grading policies, useful links on R: http://www.stat.cmu.edu/~cshalizi/statcomp
Lore for a grade-book and for turning in homework, check the class website for everything else
Matloff: textbook; required; expect to have to read some of it every week, at least for the first half
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Teetor: reference; required; like the help files, but organized by subject/task and not by command; consult it when stumped about how to do a particular thing
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Teetor: reference; required; like the help files, but organized by subject/task and not by command; consult it when stumped about how to do a particular thing
Chambers: optional; much more about details of R, good programming practices, and advanced programming techniques
Spector: optional; lots of techniques for data-manipulation
First assignments

Homework # 1 goes out Wednesday; due at the end of Thursday week after
Read introduction, chapters 1 and 2 of Matloff by Friday
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*Keep up with the readings and exercises*
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2 sorts of things (objects): data and functions
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Data: things like 7, “seven”, 7.000, the matrix \[
\begin{bmatrix}
7 & 7 & 7 \\
7 & 7 & 7 \\
\end{bmatrix}
\]
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\[
\begin{array}{cccc}
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\end{array}
\]

Functions: things like log, + (two arguments), or < (two arguments), mod (two arguments), mean (one argument)
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2 sorts of things (**objects**): **data** and **functions**

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Functions: things like log, + (two arguments), or < (two arguments), mod (two arguments), mean (one argument)

Function: a machine which turns input objects (**arguments**) into an output object (**return value**), possibly with **side effects**, according to a definite rule
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Programming is writing functions to transform inputs into outputs. Good programming ensures the transformation is done easily and correctly. Machines are made out of machines; functions are made out of functions, like \( f(a, b) = a^2 + b^2 \). The route to good programming is to take the big transformation and break it down into smaller ones, and then break those down, until you come to tasks which the built-in functions can do.
Before functions, data

Different kinds of data object
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Floating point numbers: a fraction (with a finite number of bits) times an exponent, like $1.87 \times 10^6$, but in binary form
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Missing or ill-defined values: \textbf{NA}, \textbf{NaN}, etc.
More about floating-point numbers

The more bits in the fraction part, the more precision. The R floating-point data type is a double, because the now-standard number of bits used to be twice the standard precision (back when memory was more expensive). a.k.a. numeric

Finite precision means arithmetic on doubles doesn't match arithmetic on real numbers. For example, $0.45 = 3*0.15$ is often but not always ignorable; rounding errors tend to accumulate in long calculations, particularly when results should be close to zero, since then errors could flip signs, etc. $0.45 - 3*0.15 \approx 5.551115e^{-17}$
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```r
> 0.45 == 3*0.15
[1] FALSE
```
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> 0.45 == 3*0.15
[1] FALSE
```

Often but not always ignorable; rounding errors tend to accumulate in long calculations. Particularly troublesome when results should be close to zero, since then errors could flip signs, etc.

```r
> 0.45-3*0.15
[1] 5.551115e-17
```
Unary operators: - for arithmetic negation, ! for Boolean

Binary: usual arithmetic ones, plus ones for modulo and integer division; take two numbers and give a number:

```r
> 7+5
[1] 12
> 7-5
[1] 2
> 7*5
[1] 35
> 7/5
[1] 1.4
> 7^5
[1] 16807
> 7 %% 5
[1] 2
> 7 %/% 5
[1] 1
```
Comparisons are also binary operators; they take two objects, like numbers, and give a Boolean:

```r
> 7 > 5
[1] TRUE
> 7 < 5
[1] FALSE
> 7 >= 7
[1] TRUE
> 7 <= 5
[1] FALSE
> 7 == 5
[1] FALSE
> 7 != 5
[1] TRUE
```

You can also compare strings, but that depends on R details in non-obvious ways (is And before or after an?)
Finite precision leads to weirdness with floating points and exact comparisons; `all.equal()` can usually deal with it:

\[(0.5-0.3) == (0.3-0.1)\]
al1.equal(0.5-0.3,0.3-0.1)

Boolean operators, for “and” and “or”:

\[> (5 > 7) \& (6*7 == 42)\]
[1] FALSE
\[> (5 > 7) \| (6*7 == 42)\]
[1] TRUE
More types

typeof() function returns the type
is.foo() functions return Booleans for whether the argument is of type foo:

```r
> typeof(7)
[1] "double"
> is.numeric(7)
[1] TRUE
> is.na(7)
[1] FALSE
> is.character(7)
[1] FALSE
> is.character("7")
[1] TRUE
> is.character("seven")
[1] TRUE
> is.na("seven")
[1] FALSE
```
as \texttt{foo()}\) tries to “cast” argument into something of type \texttt{foo}\) When you try to combine things of different types, R will try to convert to a type which makes sense, silently, and protest if not

\begin{verbatim}
> as.character(5/6)
[1] "0.833333333333333"
> as.numeric(as.character(5/6))
[1] 0.8333333
> 6*as.character(5/6)
Error in 6 * as.character(5/6) : non-numeric argument to binary operator
> 6*as.numeric(as.character(5/6))
[1] 5
> 5/6 == as.numeric(as.character(5/6))
[1] FALSE
\end{verbatim}

(why is that last false?)
as.foo() tries to “cast” argument into something of type foo. When you try to combine things of different types, R will try to convert to a type which makes sense, silently, and protest if not.

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> as.character(5/6)
[1] "0.833333333333333"
> as.numeric(as.character(5/6))
[1] 0.8333333
> 6*as.character(5/6)
Error in 6 * as.character(5/6) : non-numeric argument to binary operator
> 6*as.numeric(as.character(5/6))
[1] 5
> 5/6 == as.numeric(as.character(5/6))
[1] FALSE
```

(why is that last false?)
Remember you can compare strings:

```r
> as.character(5/6) > 0
[1] TRUE
> as.character(5/6) > 0.5
[1] TRUE
> as.character(5/6) > 1
[1] FALSE
> as.character(5/6) > "z"
[1] FALSE
```
Integers: subtleties

Creating a whole number in the console doesn’t make an integer; it makes a double, which just so happens to have no fractional part

> is.integer(7)
[1] FALSE

This looks just the same as an integer

> as.integer(7)
[1] 7

To test for being a whole number, use round():

> round(7) == 7
[1] TRUE
We can give names to data objects; these give us variables
A few are built in

> pi
[1] 3.141593

The assignment operator is <- or =

> approx.pi <- 22/7
> approx.pi
[1] 3.142857
> diameter.in.cubits = 10
> approx.pi*diameter.in.cubits
[1] 31.42857

Using names and variables makes code: easier to read for others,
easier to modify later, easier to design, less prone to errors
Avoid “magic constants”; use named variables
Example: resource allocation ("mathematical programming")

Factory makes cars and trucks, using labor and steel
  - a car takes 40 hours of labor and 1 ton of steel
  - a truck takes 60 hours and 3 tons of steel
  - resources: 1600 hours of labor and 70 tons of steel each week

Can it make 20 trucks and 8 cars?

\[
> 60 \times 20 + 40 \times 8 \leq 1600\tag{1}
\]
\[1\] \text{TRUE}

\[
> 3 \times 20 + 1 \times 8 \leq 70\tag{1}
\]
\[1\] \text{TRUE}

How about 20 trucks and 9 cars?

\[
> 60 \times 20 + 40 \times 9 \leq 1600\tag{1}
\]
\[1\] \text{TRUE}

\[
> 3 \times 20 + 1 \times 9 \leq 70\tag{1}
\]
\[1\] \text{TRUE}

How about 20 trucks and 10 cars?
Could just write it out *again*, but this is

- boring and repetitive
- error-prone (what if I forget to change the number of cars in line 2, or type 69 when I mean 60?)
- obscure if we come back to our work later (what are any of these numbers?)

```r
> hours.car <- 40; hours.truck <- 60
> steel.car <- 1; steel.truck <- 3
> available.hours <- 1600; available.steel <- 70
> output.trucks <- 20; output.cars <- 10
> hours.car*output.cars + hours.truck*output.trucks <= available.hours
[1] TRUE
> steel.car*output.cars + steel.truck*output.trucks <= available.steel
[1] TRUE
```

Now if something changes we just need to change the appropriate variables, and re-run the last two lines.

A step towards **abstraction**
First data structure: vectors

Group related data values into one object, a **data structure**
A **vector** is a sequence of values, all of the same type

```r
> x <- c(7, 8, 10, 45)
> x
[1]  7  8 10 45
> is.vector(x)
[1] TRUE
```

c() function returns a vector containing all its arguments in order
x[1] is the first element, x[4] is the 4th element, x[-4] is a vector containing all but the fourth element
vector(length=6) returns an empty vector of length 6; helpful for filling things up later

```r
weekly.hours <- vector(length=5)
weekly.hours[5] <- 8
```
Operators apply to vectors “pairwise”:

\[
\begin{align*}
&> y \leftarrow c(-7, -8, -10, -45) \\
&> x+y \\
&[1] 0 \ 0 \ 0 \ 0
\end{align*}
\]

**Recycling**: repeat elements in shorter vector when combined with longer

\[
\begin{align*}
&> x + c(-7, -8) \\
&[1] 0 \ 0 \ 3 \ 37
\end{align*}
\]

Single numbers are vectors of length 1 for purposes of recycling:

\[
\begin{align*}
&> x + 1 \\
&[1] 8 \ 9 \ 11 \ 46
\end{align*}
\]
Can also do pairwise comparisons:

```r
> x > 9
[1] FALSE FALSE TRUE TRUE
```

Note: returns Boolean vector

Boolean operators work pairwise; but written double, combines individual values into a single Boolean:

```r
> (x > 9) & (x < 20)
[1] FALSE FALSE TRUE FALSE
```  

To compare whole vectors, best to use `identical()` or `all.equal`:

```r
> x == -y
[1] TRUE TRUE TRUE TRUE
```  

```r
> identical(x,-y)
[1] TRUE
```  

```r
> identical(c(0.5-0.3,0.3-0.1),c(0.3-0.1,0.5-0.3))
[1] FALSE
```  

```r
> all.equal(c(0.5-0.3,0.3-0.1),c(0.3-0.1,0.5-0.3))
[1] TRUE
```
Lots of functions take vectors as arguments:

- `mean()`, `median()`, `sd()`, `var()`, `max()`, `min()`, `length()`, `sum()` all return single numbers
- `sort()` returns a new vector
- `hist()` takes a vector of numbers and produces a histogram, a highly structured object, with the side-effect of making a plot
- Similarly, `ecdf()` produces a cumulative-density-function object
- `summary()` gives a five-number summary of numerical vectors
- `any()` and `all()` are useful on Boolean vectors
Addressing vectors

Vector of indices:

> x[c(2,4)]
[1] 8 45

Vector of negative indices

> x[c(-1,-3)]
[1] 8 45

(why not 8 10?)

Boolean vector:

> x[x>9]
[1] 10 45
> y[x>9]
[1] -10 -45

which() takes a Boolean vector and gives a vector of indices for the TRUE values; useful with tests:

> places <- which(x > 9)
> y[places]
[1] -10 -45
Named components

You can give names to elements or components of vectors

```r
> names(x) <- c("v1","v2","v3","fred")
> names(x)
[1] "v1" "v2" "v3" "fred"
> x[c("fred","v1")]
fred v1
  45  7
```

note the labels; not actually part of the value

```r
> names(y) <- names(x)
> sort(names(x))
[1] "fred" "v1" "v2" "v3"
> which(names(x)=="fred")
[1] 4
```
Use vectors to group thing together

> hours <- c(hours.car, hours.truck)
> steel <- c(steel.car, steel.truck)
> output <- c(output.cars, output.trucks)
> available <- c(available.hours, available.steel)

could make it

> all(hours[1]*output[1]+hours[2]*output[2] <= available[1],
[1] TRUE

or even

> all(c(sum(hours*output), sum(steel*output)) <= available)
[1] TRUE
… but then we’d have to remember the ordering of components in each vector, and always use that order
Use names instead:

```r
> names(hours) <- c("cars", "trucks")
> names(steel) <- names(hours); names(output) <- names(hours)
> names(available) <- c("hours","steel")
> all(hours["cars"]*output["cars"] + hours["trucks"]*output["trucks"] <=
+     available["hours"],
+     steel["cars"]*output["cars"] + steel["trucks"]*output["trucks"] <=
+     available["steel"])
[1] TRUE
```
Better, but not as concise. Now try:

```r
> needed <- c(sum(hours*output[names(hours)]),
+             sum(steel*output[names(steel)]))
> names(needed) <- c("hours","steel")
> all(needed <= available[names(needed)])
 [1] TRUE
```

Not perfect programming, but better
What would we have to change to start allowing for motorcycles?
Most more complicated structures in R are made by adding bells and whistles to vectors, so “vector structures”
Most useful: arrays

> x.arr <- array(x,dim=c(2,2))
> x.arr

[,1] [,2]
[1,] 7 10
[2,] 8 45

Note: filled the first column, then the 2nd; dim tells it how many rows and columns
Can have 3, 4, … n dimensional arrays; dim is then a vector of length n
Some properties of the array:

> dim(x.arr)
[1] 2 2
> is.vector(x.arr)
[1] FALSE
> is.array(x.arr)
[1] TRUE
> typeof(x.arr)
[1] "double"
> str(x.arr)
  num [1:2, 1:2] 7 8 10 45
> attributes(x.arr)
$dim
[1] 2 2

Note: `typeof()` returns the type of the elements
Note: `str()` gives the structure: here, a numeric array, with two dimensions, both indexed 1–2, and then the actual numbers
Exercise: try all these with `x`
Can access a 2-D array either by pairs of indices or by the underlying vector:

```r
> x.arr[1,2]
[1] 10
> x.arr[3]
[1] 10
```

Omitting an index means “all of it”:

```r
> x.arr[c(1:2),2]
[1] 10 45
> x.arr[,2]
[1] 10 45
```
Using a vector-style function on a vector structure will go down to the underlying vector, *unless* the function is set up to handle arrays specially:

```r
> which(x.arr > 9)
[1] 3 4
```

Many functions *do* preserve array structure:

```r
> y.arr <- array(y,dim=c(2,2))
> y.arr + x.arr
     [,1] [,2]
[1,]   0   0
[2,]   0   0
```

Others specifically act on each row or column of the array separately:

```r
> rowSums(x.arr)
[1] 17 53
```

We will see a lot more of this idea
This class will teach you how to program for data analysis
We write programs by composing functions to manipulate data
Basic data types (Booleans, characters, numbers) and their functions
Basic data structures (vectors, arrays) and their functions
Using variables, rather than constants, is the first step of abstraction
Next time, more data structures: matrices, lists, data frames,
structures of structures