In 2016 Brent Doiron and I decided to merge my course *Statistical Models of the Brain*, which I’d taught on several previous occasions (beginning in Spring 2011), with his course *Computational Neuroscience*. Our primary motivation was to create a course for a broad range of CNBC graduate students that would represent computational neuroscience more accurately than did either of the two predecessors. Our experiences subsequently suggested some modifications of the course, but we were happy with the conception. Because Brent has left Pittsburgh, I have reduced somewhat the content he had been teaching, and I have also invited several guest lecturers to treat key topics.

Statistical ideas have been part of neurophysiology since the first probabilistic descriptions of spike trains, and the quantal hypothesis of neurotransmitter release, more than 50 years ago; they have been part of experimental psychology even longer. Throughout the field of statistics, models incorporating random “noise” components are used as an effective vehicle for data analysis. In neuroscience, however, the models also help form a conceptual framework for understanding neural function. In broad stroke, this course will examine several of the most important methods and claims that have come from applying statistical thinking and modeling to the brain. However, some of the topics use tools typically taught in statistics courses, while other topics use tools taught in math courses. Topics will involve modeling of neural activity in the sense of neurophysiology, neuroimaging, and human behavior; students will be exposed to some of each.

Even at an intuitive level, a single course can not provide a comprehensive view of computational neuroscience; the field is too broad. Instead, I have a more modest goal: I expect students, by studying a series of examples, to gain a sense of the way that computational methods contribute to contemporary understanding of neuroscience. The examples come from published papers, which, like most ideas in core course content, are old. In commentary blog posts, and in our class discussions, students are encouraged to
contribute their own thoughts about the success of these papers and the extent to which the ideas should be updated.

A detailed list of topics and assigned readings is at the end of this syllabus; however, some details will change. Please keep checking for new versions of the syllabus in Canvas.

Course Structure and Logistics

In addition to the lectures, and class discussions, the course will involve (i) the readings, (ii) student commentary blog posts on readings (often, asking questions), (iii) in-class discussion, (iv) assigned short-answer questions (SAQs) on readings, and (v) a set of small-group project presentations. There is no exam.

Students must identify themselves as either computational (for instance, if they are getting their Ph.D. in computer science, math, statistics, machine learning, neural computation, or engineering), or non-computational. Within the course, several days will be devoted to rapid overviews of mathematical and statistical methods, as background. These are aimed mainly at non-computational students, but computational students sometimes gain something of value from a new perspective on familiar material. The material in these background lectures will be covered very quickly, with the primary goal of supplying to non-computational students a conceptual understanding of the main points. Thus, non-computational students will not be expected to know or use the details. Computational students, on the other hand, should know, or study, all of the background methods in full detail, aiming at mastery. Some of the SAQs will be designated as being required only of computational students.

I plan to use a “flipped classroom” by making available a short summary lecture on each topic, so that class time can be devoted to discussion of issues raised in the student commentaries, and anything else that might arise. During class discussions I expect to begin by addressing comments and questions from non-computational students.

Grades will be based primarily on student commentary (which requires thoughtful engagement with the readings) and short-answer questions (which will be aimed at pulling out the biggest points from the readings and lectures). Specifically, 75% of the grade will be based on commentary and short-answer questions, with the remaining 25% based on the project. Please note: all deadlines must be met: students will be penalized (possibly severely) for failing to hand assignments in on time, or for failing to propose their project on time (see below). The TA for the course is Nour Riman nourr@andrew.cmu.edu.

The course is heavy on readings. I hope that students will spend the time it takes to digest each assigned article thoroughly. However, knowing that time is limited, I require
only that students (a) post a cogent comment or question on the discussion board and (b) answer the SAQs.

A few details:

- The course will be run through the CMU hosting of 36-759 on Canvas, see https://canvas.cmu.edu.

- Comments on readings must be posted on the appropriate discussion forum no later than 10am on the assigned day of class. Students will have access to commentary by others only after they post themselves. The instructor will read these posts prior to class, and use them to guide the lecture overview.

Comments are meant to demonstrate engagement with the material, and will be graded on a 0/1/2 basis, with 1 signifying a minimal response. Comments may consist entirely of questions identifying points not yet clear to the student. In my experience there is a lot of variation in length, but typically a few sentences will suffice. Here are 4 examples of student comments on one of the readings:[1]

- The building, computer, brain analogy is very instructive. It’s interesting to see the shift in perspective where before the trend was to think of the brain as like a computer whereas now the trend is to make a computer operate like the brain. The explanation of three shortcuts made the concept of the cognitive architecture easy to grasp. The modular break up of ACT-R was very informative. The results shown in Figure 1.6 are impressive. I didn’t quite catch what figure 1.7 is trying to show. [SCORE: 2]

- Anderson presents a rather attractive metaphor for how he sees it best to approach understanding the brain, one that could be well summed up as, “the whole is greater than merely the sum of its parts.” That idea that you can’t simply deconstruct ad infinitum in one direction and work your way back to the other side seems deeply sobering. Taken to its logical conclusion though, I wonder whether if in accepting what could be perceived as Anderson’s principal conclusions, one must also find it unsatisfying as it might be that the best that can be achieved is a model of our cognitive architecture, which can only be refined and improved, but that never quite gets there. [SCORE: 2]

- I thought the Anderson chapter was really interesting and easy to read. The example in Figure 1.8 (using module behavior to predict BOLD response) was

[1] The scores here are retrospective, for illustration.
particularly interesting and really pulled together the concepts of ACT-R and how we can use it to understand brain function. [SCORE: 2]

– Not convinced... too philosophical to be science. [SCORE: 1]

• Each SAQ based on readings (and the relevant lecture about the readings) will require students to submit an answer of roughly 1 to 3 sentences in length. These will be managed and self-graded, with random spot-checks, using the Canvas quiz tool. The SAQs MUST be answered by each student working independently, and they MUST be answered within a specified 48 hour window. Students will be notified when the window opens. The syllabus informs students of the primary learning objectives most relevant to the SAQs by indicating key sections to “pay attention to.” This will help guide students in reading. In addition, the SAQs will be handed out 5 days prior to the opening of the window (except for the first SAQ, which is based only on the first substantive lecture).

• Because much of the course will move very fast, students should try to read ahead when possible.

• I plan to make pre-recorded lectures available at least 2 days prior to the class meeting time. It is advisable to watch the lecture prior to submitting a comment. If pre-recorded lectures are not available (e.g., for guest lecturers), lecture slides will be made available.

• Projects by students, working in teams of 3 students (with occasional exceptions in size of team) will be handed in as narrated slides, in PowerPoint. These voice-over recorded presentations must run between 10 and 15 minutes, in total. The subject of the project should be a summary of 1 or more papers. All students must attend the presentation sessions, which will be on May 12 and 14, and must send their presentation to the TA by 5:00pm, Monday, May 10. At the session, the presentation will be played and the students will very briefly answer questions. Students must have their project approved by the instructor no later than Wednesday April 7. To get approval, students must submit a proposal by email message to the TA (no other document is required) that includes (1) the team of 3 people who will do the project (all team members must submit their own email); (2) the topic, described in several sentences including reference to the paper or papers that will be discussed; and (3) what work each student will be responsible for—all students are responsible for the whole finished product, but, for example, only 1 student typically will record the narration. In some cases proposals will have to be revised. For this reason, each student must submit such an email to the TA no later than Thursday April 1.
A key text for statistical tools is *Analysis of Neural Data*, Kass, Eden, and Brown (KEB), published by Springer. Information about the book is at [http://www.stat.cmu.edu/~kass/research.html#and](http://www.stat.cmu.edu/~kass/research.html#and). NOTE: a pdf version of the book is free for both CMU and Pitt students. Also, please check the extensive list of corrections at [http://www.stat.cmu.edu/~kass/KEB/corrections2021.pdf](http://www.stat.cmu.edu/~kass/KEB/corrections2021.pdf). Students who have weak backgrounds in neurophysiology should find a basic source on neurons and read it. I recommend the first 5 chapters of Bear, Connors, and Paradiso *Neuroscience: Exploring the Brain*, which assumes only high-school biology.

**Accommodations for Students with Disabilities**

If you have a disability and have an accommodations letter from the Disability Resources office, we encourage you to discuss your accommodations and needs with one of the instructors as early in the semester as possible. We will work with you to ensure that accommodations are provided as appropriate. If you suspect that you may have a disability and would benefit from accommodations but are not yet registered with the Office of Disability Resources, we encourage CMU students to contact them at access@andrew.cmu.edu. Pitt students should contact Disability Resources and Services (DRS), 216 William Pitt Union, (412) 648-7890/(412) 383-7355 (TTY).

**Support for Health and Well-being**

Take care of yourself. Do your best to maintain a healthy lifestyle this semester by eating well, exercising, avoiding drugs and alcohol, getting enough sleep and taking some time to relax. This will help you achieve your goals and cope with stress. All of us benefit from support during times of struggle. There are many helpful resources available on campus and an important part of the college experience is learning how to ask for help. Asking for support sooner rather than later is almost always helpful. If you or anyone you know experiences any academic stress, difficult life events, or feelings like anxiety or depression, we strongly encourage you to seek support. At CMU, Counseling and Psychological Services (CaPS) is here to help: call 412-268-2922 and visit their website at [http://www.cmu.edu/counseling/](http://www.cmu.edu/counseling/). Consider reaching out to a friend, faculty or family member you trust for help getting connected to the support that can help.
Topics and Readings

NOTES: (1) Comments are required on all readings unless otherwise indicated. (2) The SAQs will be based on the material indicated as needing special attention. (3) Some details will change, especially involving the material for SAQs, which for later topics may not yet be indicated, so watch for updates.

0. Feb 3 Overview: The nature of statistical models of the brain; as an example, Bayes' theorem and its uses; class structure, including readings, questions, comments, and homework.

1. Feb 5 What is computational neuroscience?
   

   **Required video:** [https://www.youtube.com/watch?v=4iPeV_o5f9Y](https://www.youtube.com/watch?v=4iPeV_o5f9Y)

   **Pay special attention:** the brain-as-computer metaphor; Marr’s three levels of analysis; tuning curve video.

   **SAQ1 Window:** Feb 7-9.

2. Feb 10 Random variables; What is a statistical model? Fitting statistical models to data.
   
   **Required reading:** Kass, Eden, Brown (KEB), Chapter 1, especially 1.2.1; Chapter 3 through Equation (3.1); Section 3.2 through 3.2.3 (reminder to see corrections).

   **Pay special attention:** “Signal” and “noise” in Examples 1.4 and 1.5; Equation (1.4).

   **Computational students, in addition:** Read the rest of Chapter 3, especially 3.2.4 (reminder to see corrections); pay attention to Figure 1.1; Sections 1.2.5, 1.2.6 (see also Section 8.1), 3.2.4.

3. Feb 12 Background: Log transformations; random vectors; important probability distributions and the way they model variation in data.

   **Reading:** KEB Ch 2, esp. 2.2.1; Ch 4 through 4.2.2; 4.3.1 through Equation (4.26); 5.1-5.3; 5.4.2.

   **Attention:** Secs 2.2.1, 5.2.1, 5.4.2; Figs 2.5, 2.6.

   **Comp students:** read the rest of 4.3.1 and Ch 5; Attention: Secs 4.2.4, 5.5.
4. Feb 17  RK. *Background:* The Law of Large Numbers and the Central Limit Theorem; statistical estimation; least-squares linear regression and the linear algebra concept of a basis.

*Reading:* KEB Ch 6 through 6.1.1; 6.2.1; 7.1, 7.2, 7.3.1; Introduction to Ch 12; 12.5 through 12.5.1; appendices A.7 and A.9; 12.5.3 through equation (12.57) on p. 342; 12.5.8.

*Attention:* 6.2.1; Fig 7.2; Introduction to 12.5 and 12.5.8; A.7; Fig 12.9 (which is the same as the bottom of Fig A.2).

*Comp students:* 6.1.2, 6.3.2; 12.5.5, 12.5.7; A.8; attention to 12.5.7. Secs 7.3.8, 7.3.9 are recommended.

5. Feb 19 Random walk models of integrate-and-fire neurons; effects of noise: balanced excitation and inhibition.

*Readings:* KEB Sec 5.4.6; Introduction to Ch 19.


Stein, R.B., Gossen, E.R., and Jones, K.E. (2005) Neuronal variability: noise or part of the signal? *Nat. Rev. Neuro.*, 6:389-397. *Only Figure 1 and Figure 2, pp. 390-391.* The histograms are explained by this statement on p. 392, “The ability of the neuron to transmit signals faithfully is only evident after analysing many cycles of the stimulus. However, transmission by a population of neurons, rather than a single neuron, would allow the signal to be evident in real time.” See my video lecture for a bit more on this.

*Attention:* Shadlen and Newsome, “price of dynamic range is noise,” Fig 2; Stein et al., Fig 2.

*Comp students:* KEB Secs 19.1-19.2; attention to the theorem in 19.2.1.


*Readings:* KEB, Sec 12.5.4.


Attention: KEB, Example 12.6; Figure 2 of Georgopulos et al.; Equation (5) of Black and Donoghue.

7. Feb 26 Information theory in human discrimination.

**Background Reading:** KEB Section 4.3.2, especially comments about entropy and channel capacity, pp. 95-97, including Examples 4.5 and 4.6.


Attention: KEB Example 4.6; Miller, Figure 2.

8. Mar 3 Nour Riman. **Background:** Ideas in differential equations and dynamical systems.

**Video:** [https://www.youtube.com/watch?v=p_di4Zn4wz4](https://www.youtube.com/watch?v=p_di4Zn4wz4)

Here are some questions that should help you better understand the video:

Q1. Under what circumstances are differential equations used?
Q2. What is the order of a differential equation?
Q3. What is a phase space?
Q4. What is an attracting state?


**Reading:** Ermentrout and Terman (2010) *Mathematical Foundations of Neuroscience*, Springer. Secs 1.1-1.5 (an electronic version of this book is freely available to all Pitt and CMU students).

Attention: Nernst equation and how it differs from GHK equation; time constant of RC model.


Attention: voltage clamp; distinction between sodium and potassium conductances.

11. Mar 12 Jon Rubin. Network dynamics. **COMMENTS DUE AT 7:30 am on March 12**

Attention: From network perspective, advantages of ongoing activity due to balanced excitation and inhibition (as in Figure 3 d,e).

SAQ2 Window: Mar 14-16.

12. Mar 17 Background: Bayes’ Theorem; optimality of Bayesian classifiers; mean squared error; Bayes and maximum likelihood.
   Reading: KEB Secs 4.3.3-4.3.4 through p. 101; 8.1-8.2; 8.3.3.
   Attention: Theorem on p. 182; Equation (8.10); Figure 8.8.

Mar 19 NO CLASS (CMU break)

13. Mar 24 Cognition and optimality; ACT-R.
   Background reading: KEB, pp. 102-103, through Example 4.9.
   Attention: Anderson’s three “shortcuts”

14. Mar 26 Background: statistical tests, ROC curves, signal detection theory.
   Reading: KEB Chapter 10 up to the beginning of Sec 10.1.1 (p. 249); Secs 10.4.1; 10.4.3-10.4.4, especially Figure 10.3.
   Comp students: The rest of Chapter 10.
   Attention: Figures 10.3 and 10.4.

NOTE Projects have been canceled!

15. Mar 31 Optimal observers in perception and action.
   Background reading: KEB Chapter 16 through equation (16.18) on p. 449, especially Example 16.1; see also Example 8.1.
   Attention: KEB, Equations (16.11), (16.12); Körding and Wolpert Figure 2.

16. Apr 2 Background: Regression and generalized regression.
   Reading: KEB Chapter 14 through 14.1 (can skip 14.1.2, 14.1.5); 15.2 through 15.2.4.
17. Apr 7 Firing rate and neural coding; spike trains as point processes.

*Reading:* KEB Example 14.5, pp. 410-411; Chapter 19 through page 569.

*Comp students:* check the rest of Ch 19, and read what interests you; read Sections 1 and 2, and Figures 6 and 9, of Weber and Pillow (2017).


*Attention:* the 3 types of point processes identified in the lecture as needed for the next reading.

*Comp students:* KEB Figure 19.9 and Weber and Pillow Figure 9.

18. Apr 9 Information theory in neural coding.

*Background reading:* KEB, Example 4.6.


*Attention:* Figure 3 of Nirenberg et al. and Figure 2 of Jacobs et al.


**SAQ3** Window: April 11-13.

19. Apr 14 Neural implementation of Bayesian inference.


*Attention:* Figure 1 of Salinas.
Apr 16 NO CLASS (CMU break)


*Background reading:* KEB, Example 6.1, p. 141 (review), and Section 17.3.1, especially the examples.


*Attention:* Figure 1 of Averbeck, Latham, Yu and Figures 1 and 2 of Cunningham and Yu.

21. Apr 23 Neural basis of decision making.

*Background reading:* KEB, Section 11.1.5 and the discussion of SDT in Section 10.4.4.


*Attention:* Figures 4 and 5c.

22. Apr 28 Chencheng Huang. Network models of decision-making.


23. Apr 30 Reinforcement learning.

*Reading:* Glimcher, P. (2011) Understanding dopamine and reinforcement learning: The dopamine reward prediction error hypothesis, *PNAS*, 108: 15647–15654 (with corrections, pp. 17568–17569), through the interpretation of Figure 3.

*Attention:* Figures 2 and 3.


Attention: Graphical abstract and Figure 7 (the methods are explained, briefly, in the video lecture).


25. May 7 What is science?

video: [https://www.youtube.com/watch?time_continue=4&v=PwCyvSDkUCY&feature=emb_logo](https://www.youtube.com/watch?time_continue=4&v=PwCyvSDkUCY&feature=emb_logo)


**SAQ4** Window: May 9-11.

May 12 and 14 **PROJECTS CANCELED**