

$$L(x, u, v) = -\infty \text{ whenever } u \neq 0$$

$$\begin{aligned} \text{QP: } L(x, u, v) &= f(x) + \sum u_i \cdot (-x_i) + \sum v_j (a_j^T x - b_j) \\ &= f(x) - u^T x + v^T (Ax - b) \\ &= \frac{1}{2} x^T Q x + c^T x + \underbrace{\quad \quad \quad} \\ &= \frac{1}{2} x^T Q x + (c - u + A^T v)^T x - b^T v \end{aligned}$$

$$g(u, v) = \min_x L(x, u, v)$$

minimizer:

$$-Q^{-1}(c - u + A^T v)$$

$$\begin{aligned} ax^2 + bx + c \\ -b/2a \end{aligned}$$

Quartic

$$L(x, u) = x^4 - 50x^2 + 1000x - ux - 4.5u$$

$$g(u) = \min_x L(x, u)$$

$$4x^3 - 100x + 1000 - u$$

Ups:

primal.

Slater's: if feasible then
 $f^* = g^*$

dual

Slater if feasible

$$g^* = f^*$$

$$\begin{array}{l|l} -\xi_i \leq 0, \quad i=1..n & v_i \geq 0 \\ \hline 1 - \xi_i - y_i(x_i^T \beta + \beta_0) \leq 0 & w_i \geq 0 \\ i=1..n & \end{array}$$

min β, β_0, ξ

$$\frac{1}{2} \beta^T \beta - \sum y_i w_i x_i^T \beta - (\sum y_i w_i) \beta_0 + \sum w_i + \sum (C - v_i - w_i) \xi_i$$

over β_0 : get constraint $w^T y = 0$

over ξ : get constraints $w_i = C - v_i$
 $i=1..n$

over β :

$$\frac{1}{2} \beta^T \beta - w^T \tilde{X} \beta$$

minimizer: $\tilde{X}^T w$

min val: $-\frac{1}{2} w^T \tilde{X} \tilde{X}^T w$

\tilde{X} is X with ^{rows} ~~cols~~ scaled by y