

The Velocity Distribution Function of Galaxy Clusters as a Cosmological Probe

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Image credit: nasa.gov

dunkle Materie

Scheinbare Geschwindigkeiten im Comahaufen.

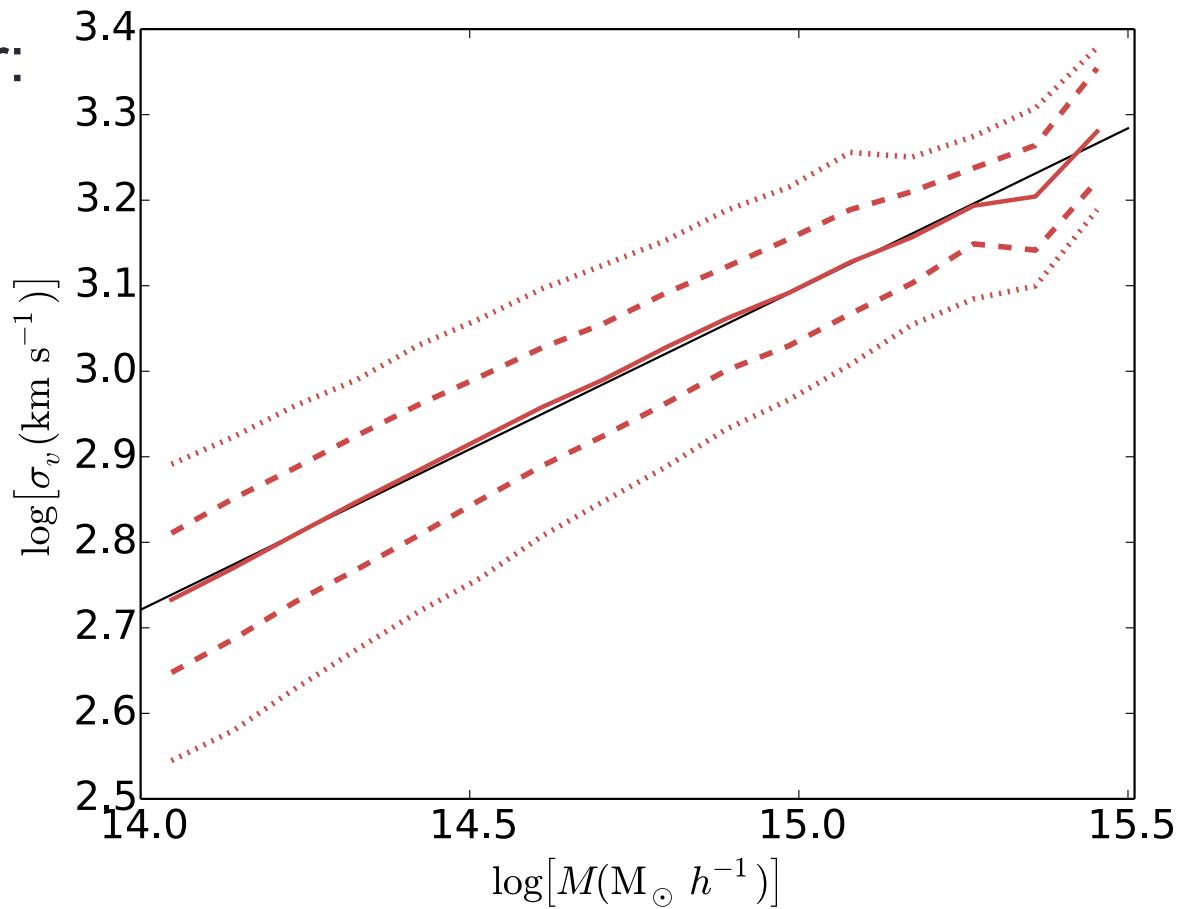
$v = 8500$	km/sek	6900	km/sek
7900		6700	
7600		6600	
7000		5100	(?)

Sources of Scatter in Dynamical Mass Estimates

From the virial theorem, $\sigma_v \propto M^{1/3}$

Sources of scatter:

- Mergers
- Infalling matter
- Halo triaxiality
- Observational effects



Multidark Simulation

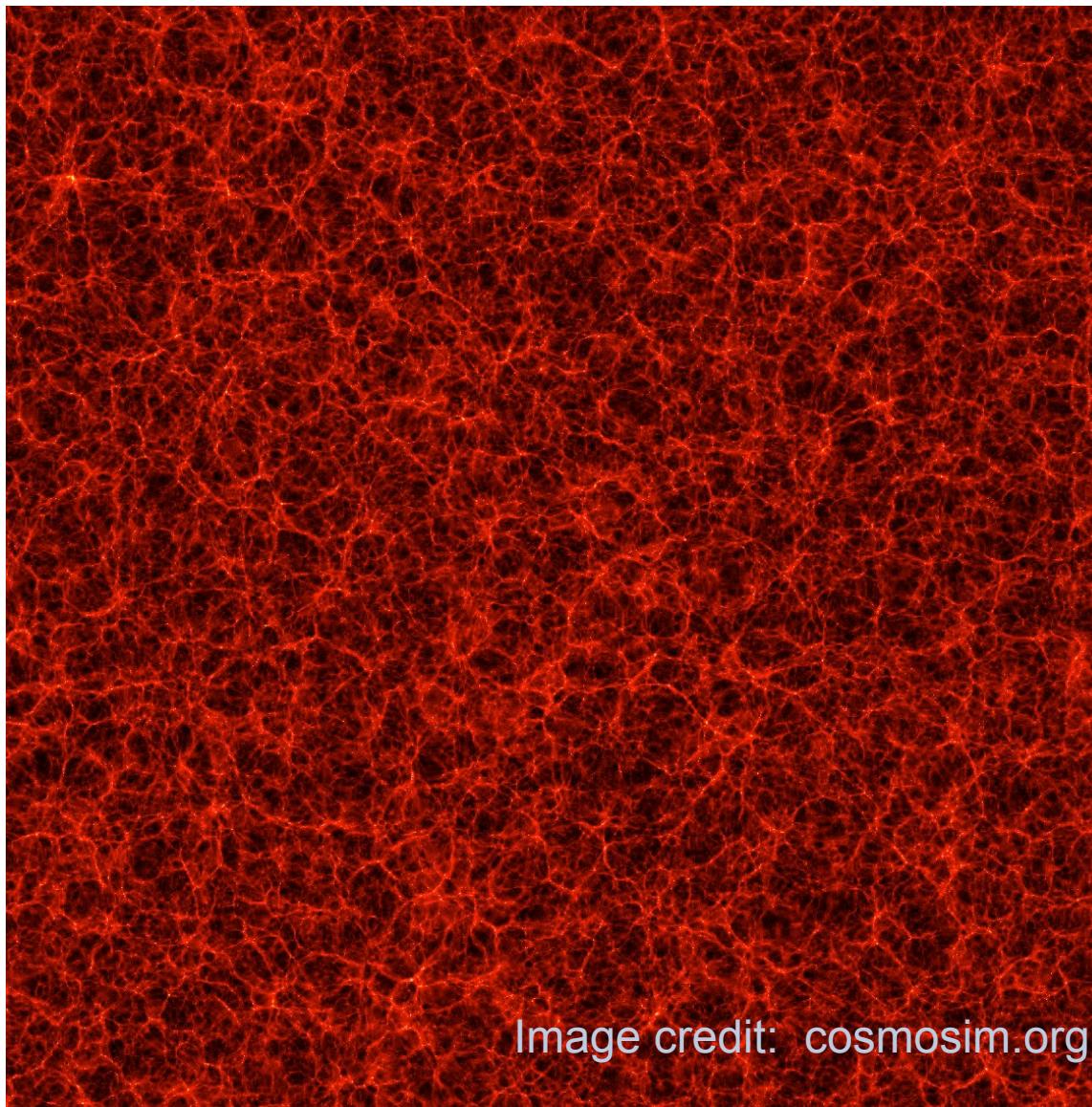
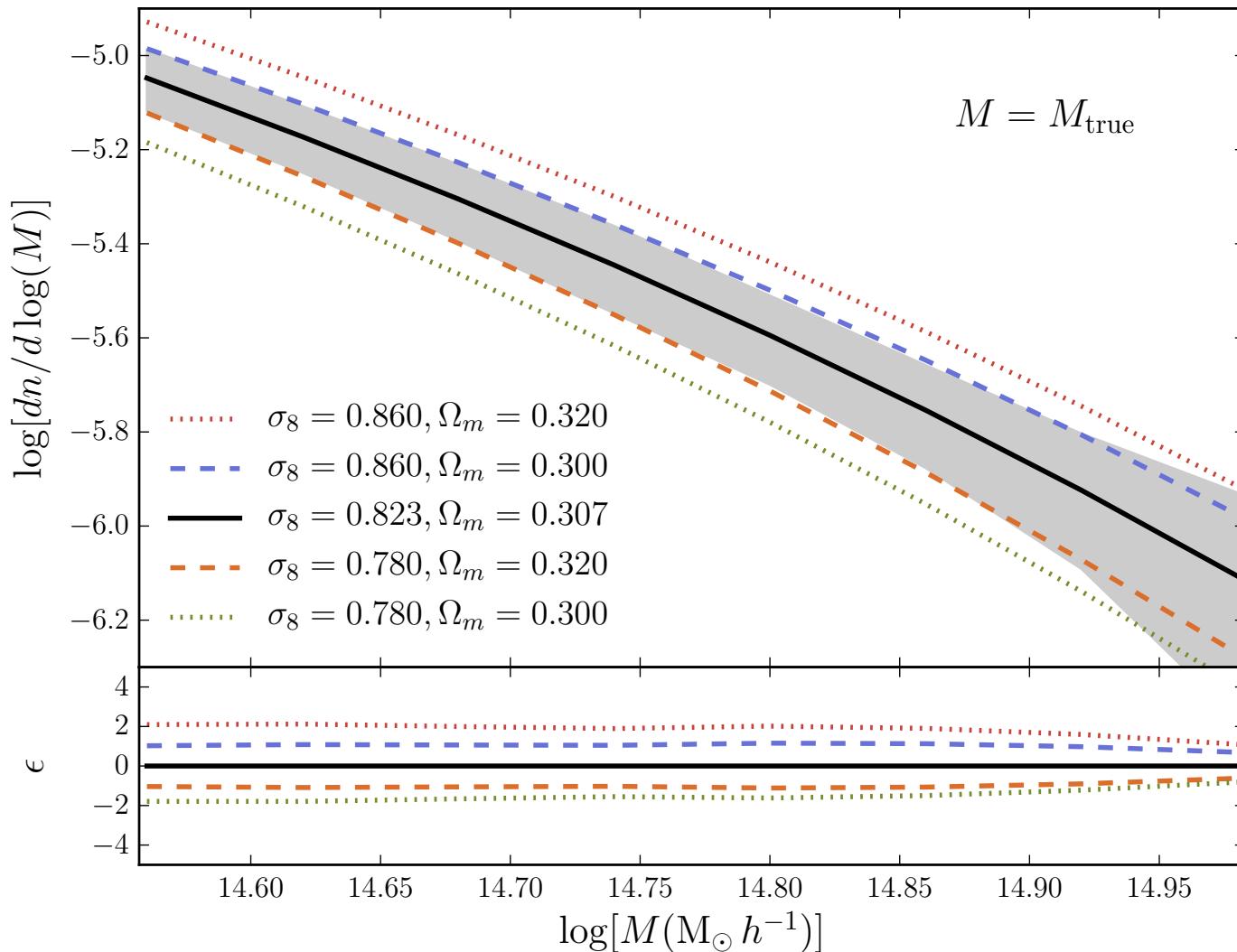


Image credit: cosmosim.org

HALO MASS FUNCTION

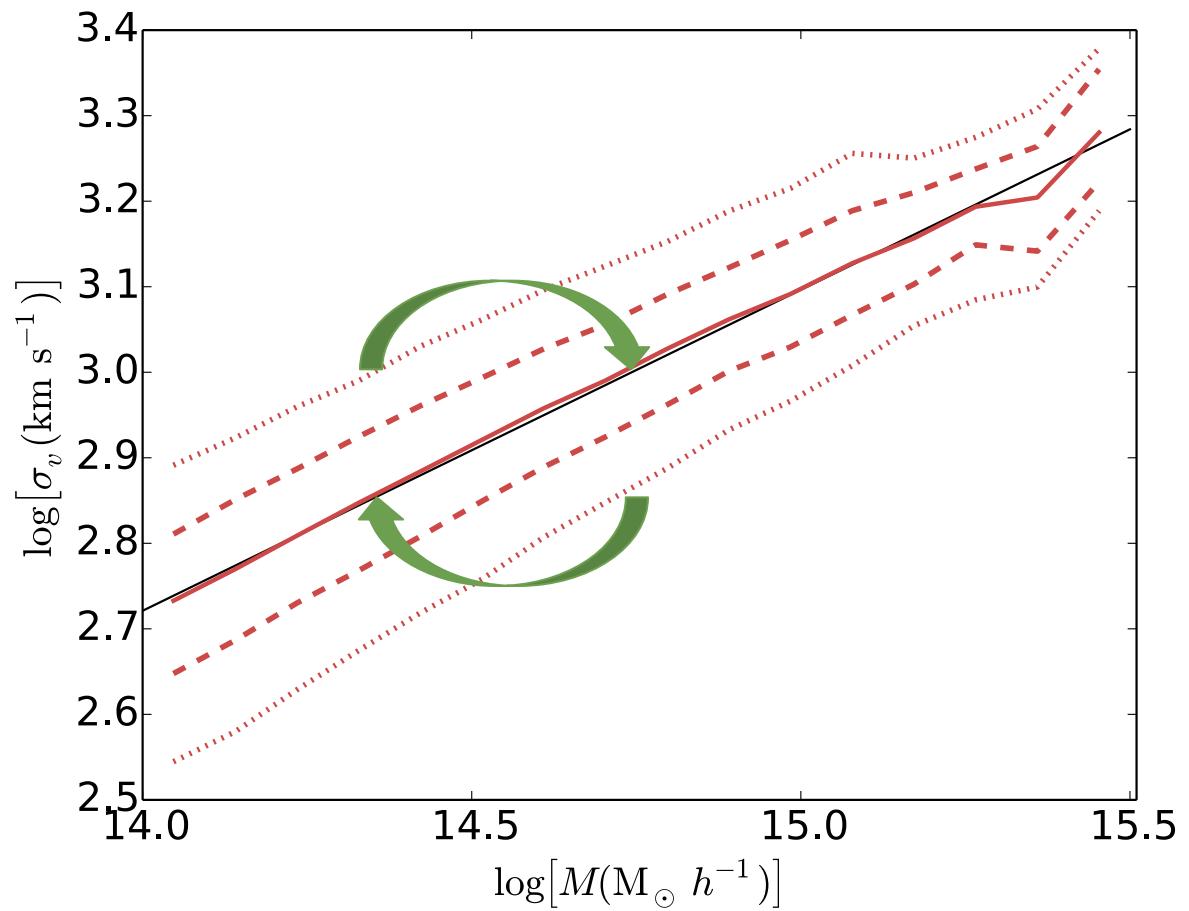
It's impolite to ask a galaxy cluster its mass

Halo Mass Function

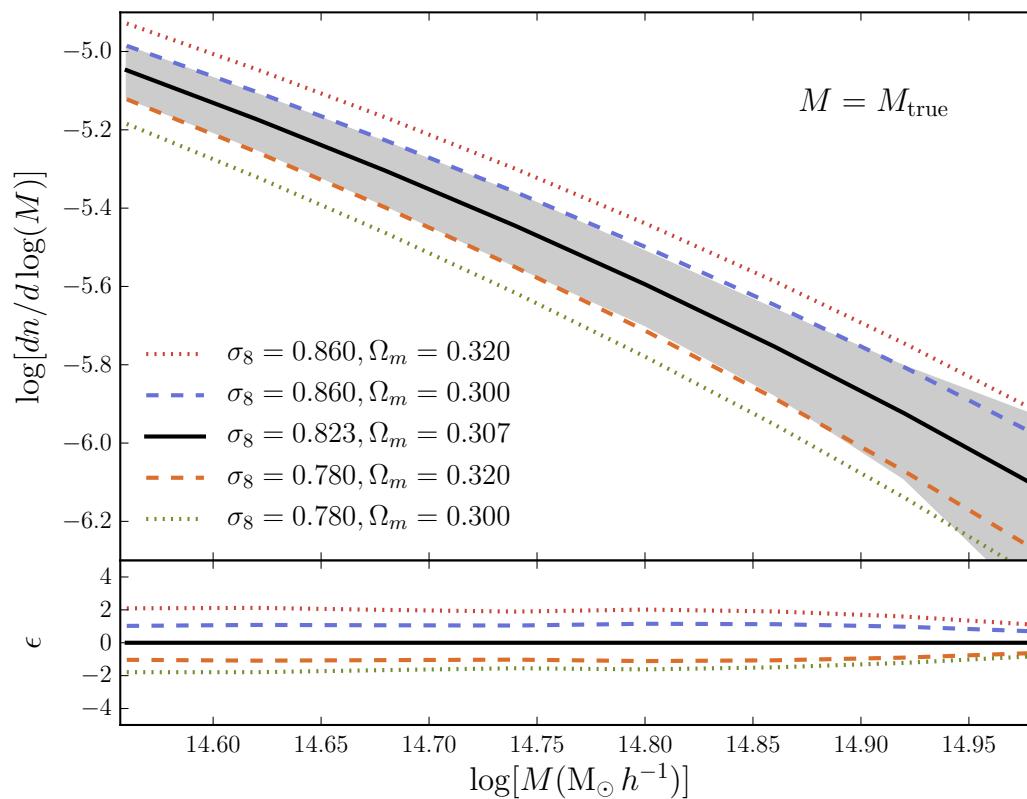


Eddington Bias in Dynamical Masses

Scatter in the $M(\sigma)$ relationship, coupled with the steeply-declining HMF, alters the observed HMF.

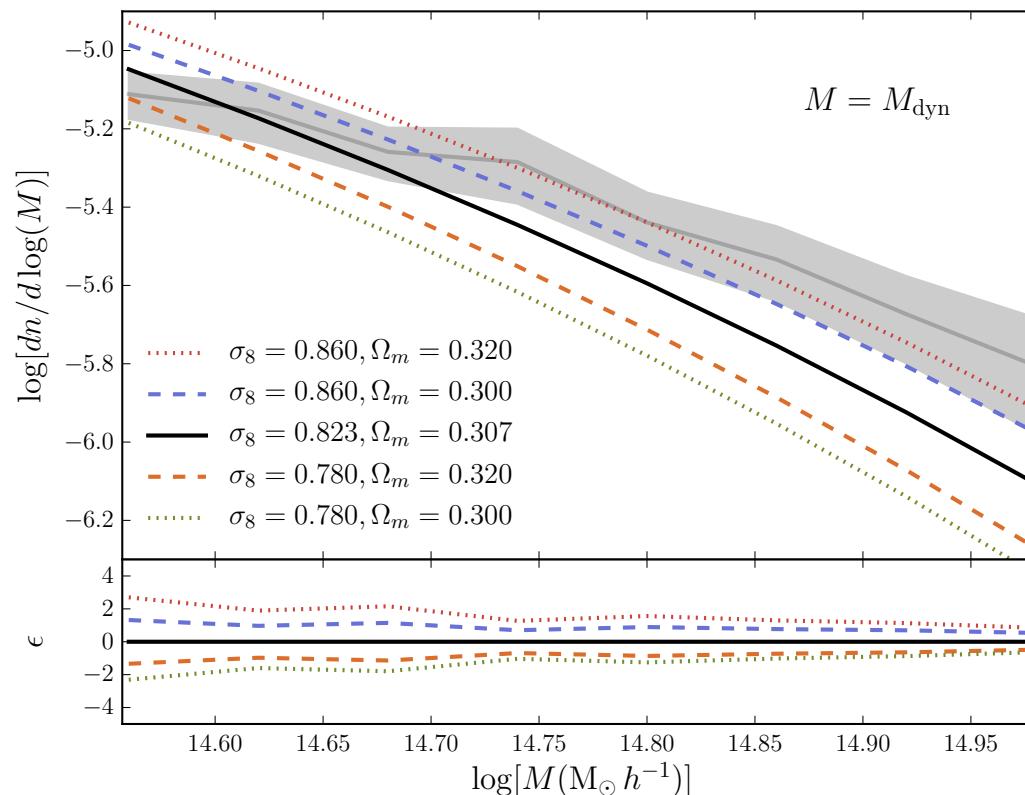


Halo Mass Function



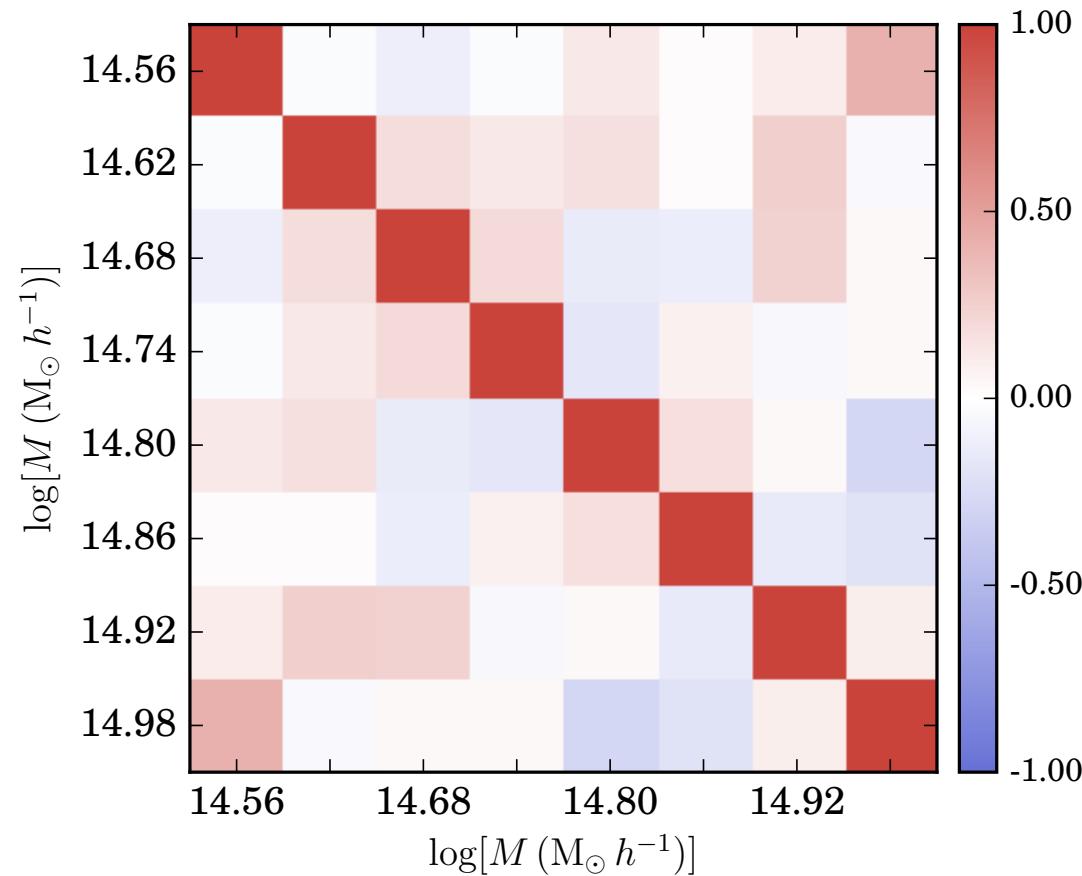
Halo Mass Function with Measurement Error

- True mass function can be recovered if the scatter is well-understood.



χ^2 analysis for constraining σ_8 & Ω_m

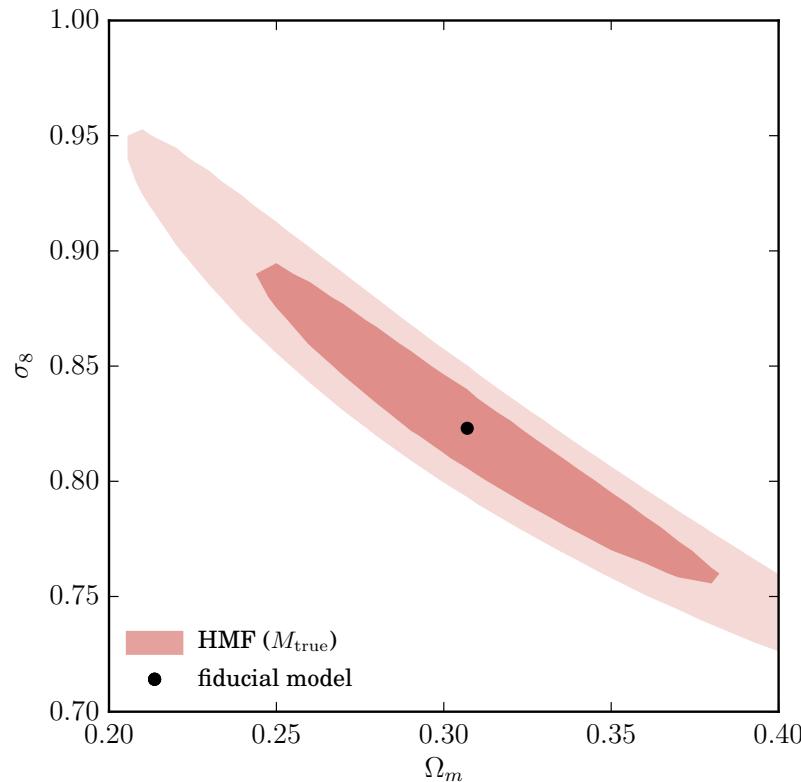
$$\chi^2(y|\sigma_8, \Omega_m) = (\bar{y} - y^\star)^T \hat{\Psi}^{-1} (\bar{y} - y^\star)$$



- Compare the mock observed HMF to that predicted by an analytic HMF.

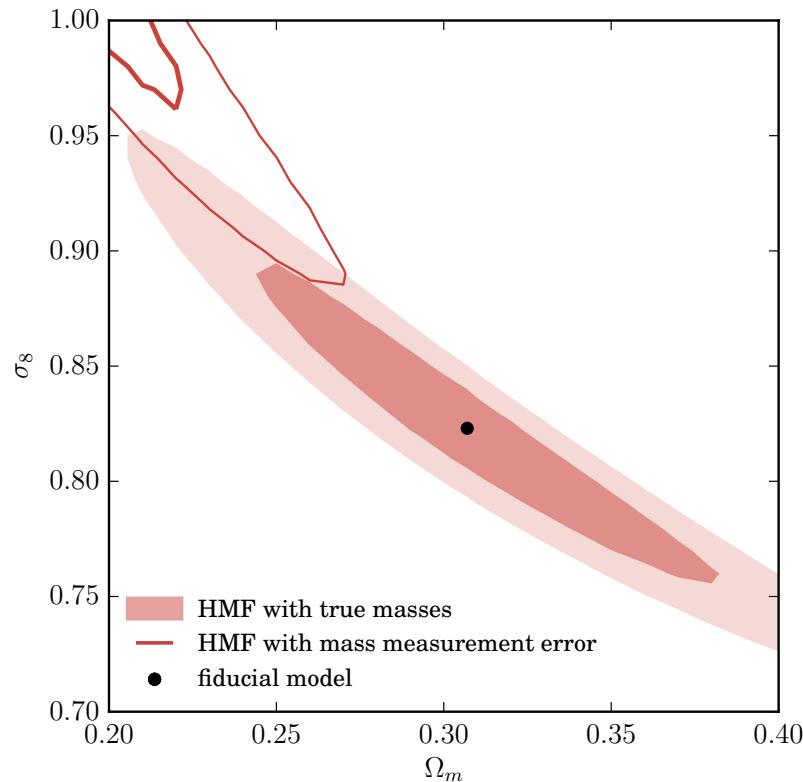
Constraining Cosmological Models

- When cluster masses are perfectly known, the parameter constraints contain the fiducial model.



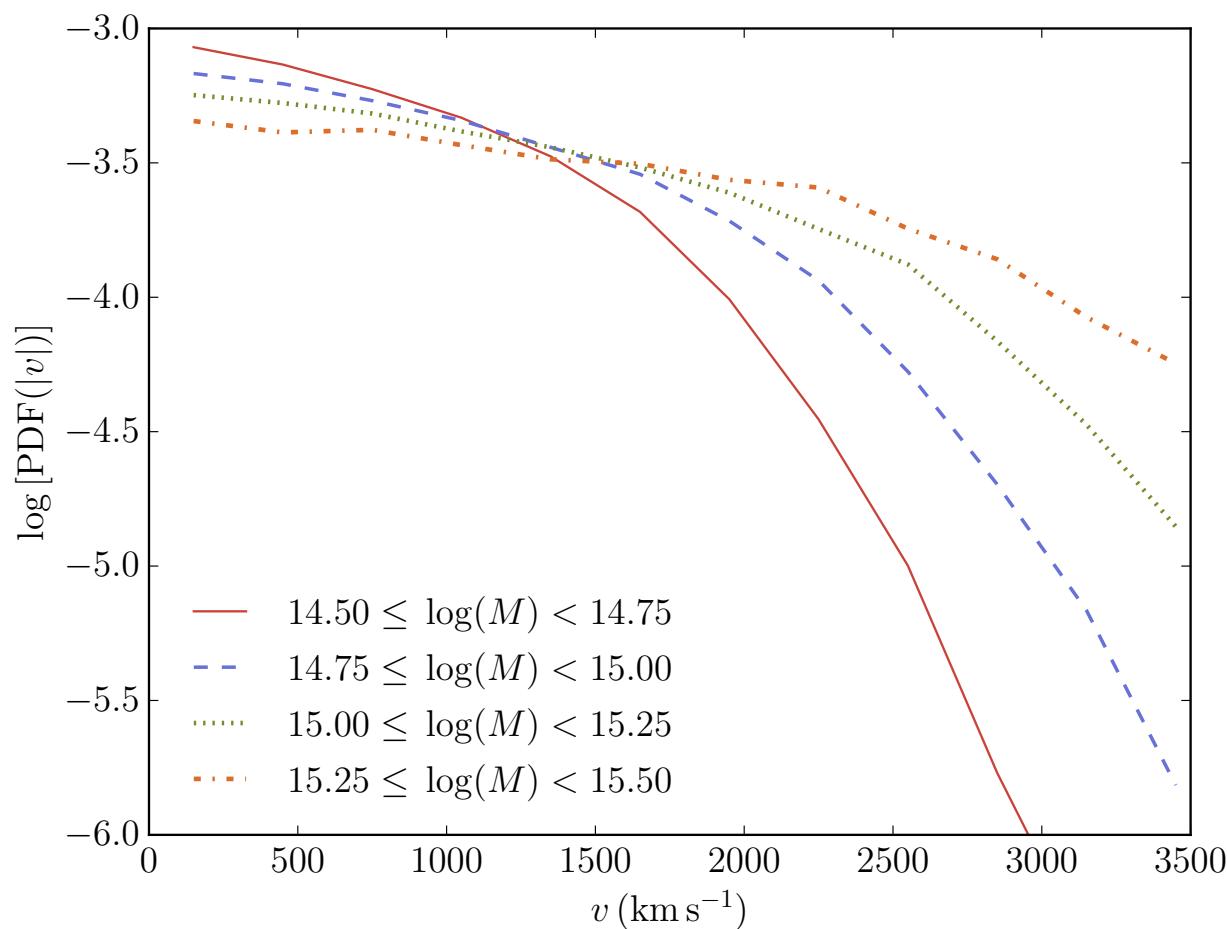
Constraining Cosmological Models

- Measurement error biases to low Ω_m and high σ_8 .
- Fiducial model lies outside of the 99% likelihood contour.

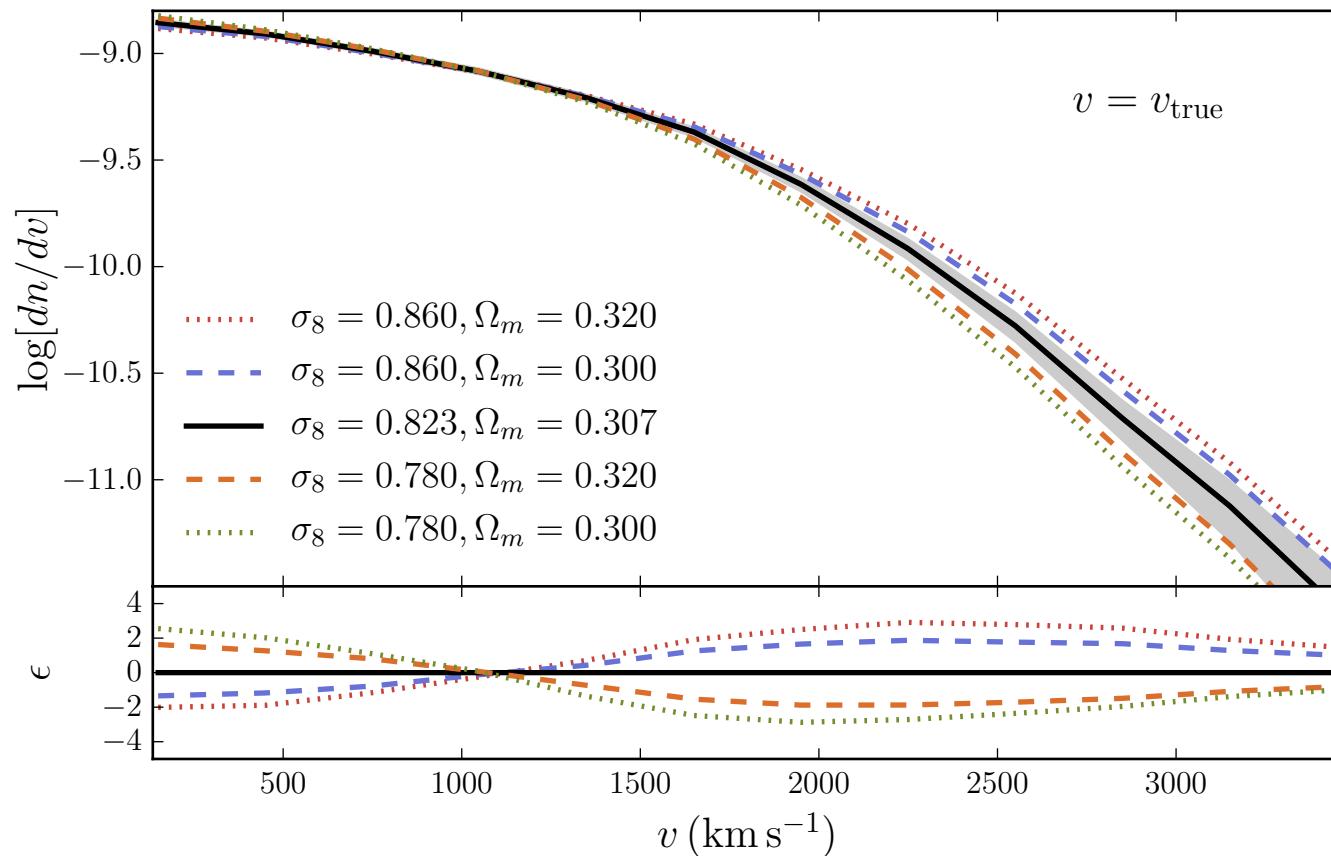


THE VELOCITY DISTRIBUTION FUNCTION

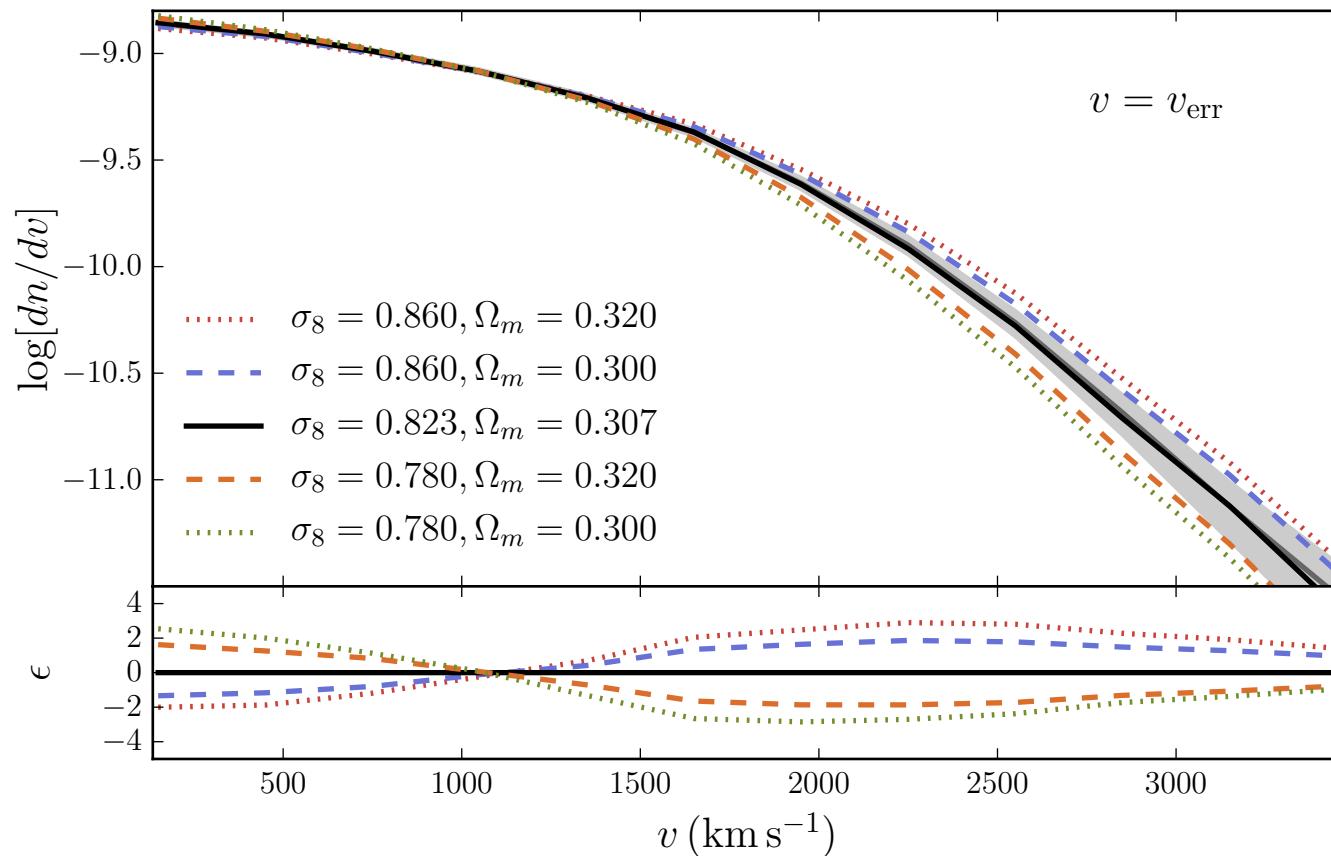
Velocity PDF



Velocity Distribution Function

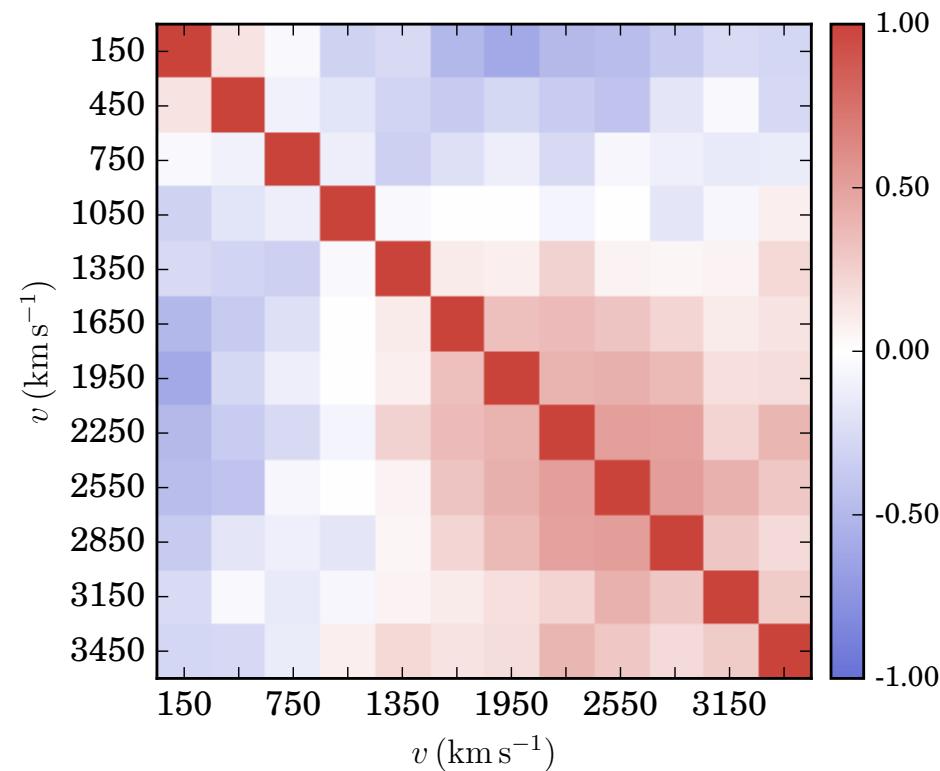


Velocity Distribution Function with velocity error



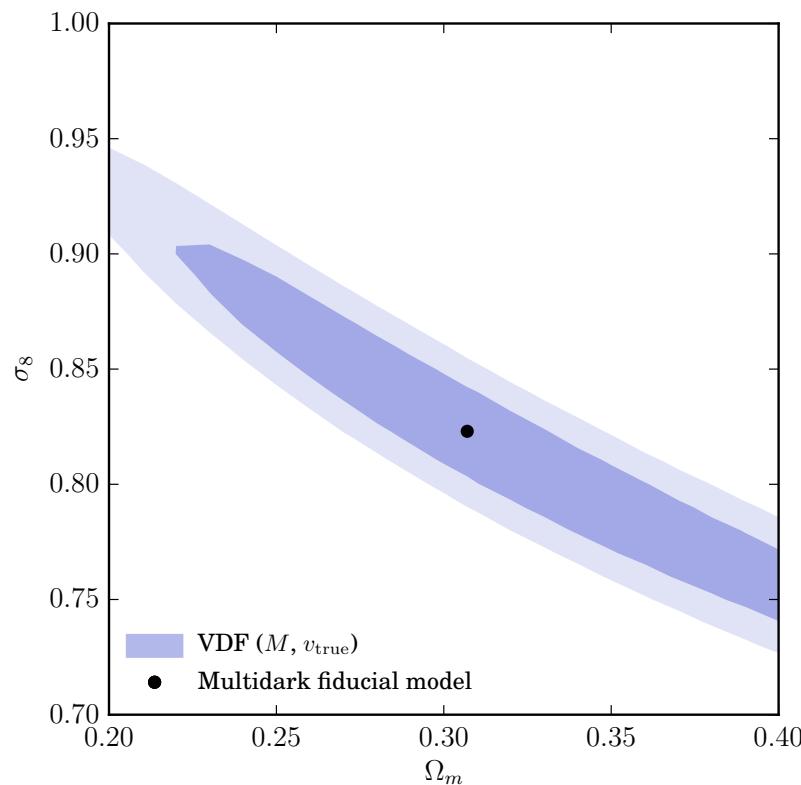
χ^2 analysis for constraining σ_8 & Ω_m

$$\chi^2(y|\sigma_8, \Omega_m) = (\bar{y} - y^\star)^T \hat{\Psi}^{-1} (\bar{y} - y^\star)$$



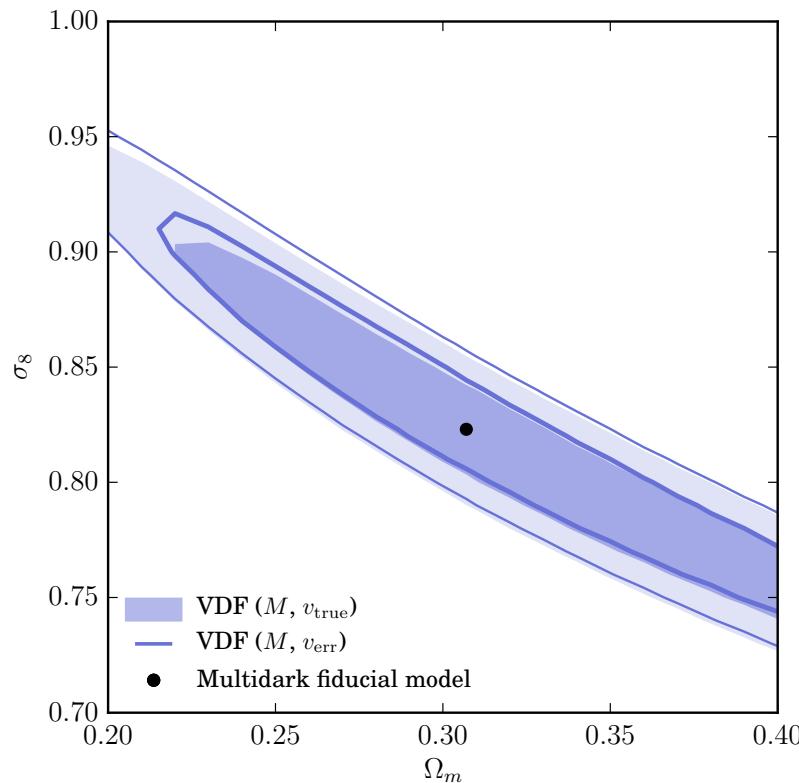
Constraining Cosmological Models with the VDF

- Constraints can be approximated as a band in the Ω_m - σ_8 plane.



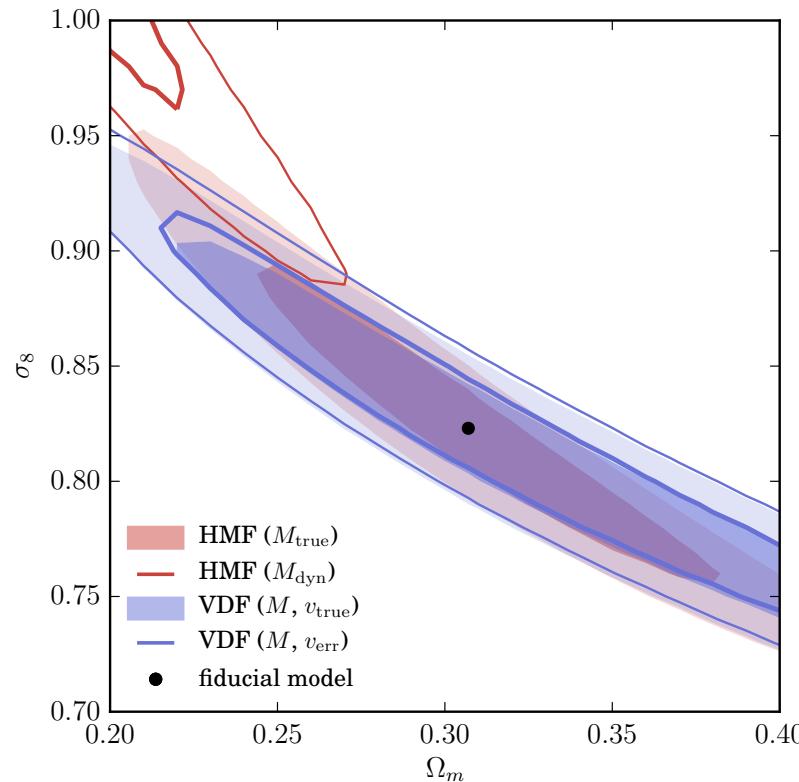
Constraining Cosmological Models with the VDF

- Measurement error introduces a nearly-negligible bias.



Constraining Cosmological Models with the VDF

- HMF and VDF give similar constraints *when true cluster properties are known.*
- VDF is less sensitive to measurement error than the HMF.



- Can be robustly predicted from N -body simulations that capture dynamics of substructure in clusters.
- Applying the VDF requires a large spectroscopic data set of cluster members.
- Applying the VDF to smaller observations ($N < 200$) retains the insensitivity to measurement error, though with broader constraints.

The Velocity Distribution Function of Galaxy Clusters

- A new way to quantify the abundance of galaxy clusters using dynamic measurements ([arxiv: 1602.01837](#)).
- Less sensitive to systematics than a more traditional halo mass function approach where scatter in mass estimate introduces bias.