

Lab 5: Testing Our Way to Outliers

36-350, Statistical Computing

28 September 2012

Agenda: Debugging and testing; finding outliers.

Instructions: Save all your answers in a single plain text file (Word files will not be graded), and upload it to Lore. When a question asks you to do something, give the command you use to do it. For questions which ask you to explain, write a short explanation in coherent, complete sentences. (You will be graded on your written explanation, not what you might say to the TA.)

Identifying outliers in data is an important part of statistical analyses. One simple rule of thumb (due to John Tukey) for finding outliers is based on the quartiles of the data: the first quartile Q_1 is the value $\geq 1/4$ of the data, the second quartile Q_2 or the median is the value $\geq 1/2$ of the data, and the third quartile Q_3 is the value $\geq 3/4$ of the data. The interquartile range, IQR , is $Q_3 - Q_1$. Tukey's rule says that the outliers are values more than 1.5 times the interquartile range from the quartiles — either below $Q_1 - 1.5IQR$, or above $Q_3 + 1.5IQR$.

Consider the data values

```
x <- c(2.2, 7.8, -4.4, 0.0, -1.2, 3.9, 4.9, -5.7, -7.9, -4.9, 28.7, 4.9)
```

We will use these as part of writing a function to identify outliers according to Tukey's rule. Our function will be called `tukey.outlier`, and will take in a data vector, and return a Boolean vector, `TRUE` for the outlier observations and `FALSE` elsewhere.

1. (5) Calculate the first quartile, the third quartile, and the inter-quartile range of `x`. Some built-in R functions calculate these; you cannot use them, but you could use other functions, like `sort` and `quantile`.
2. (10) Write a function, `quartiles`, which takes a data vector and returns a vector of three components, the first quartile, the third quartile, and the inter-quartile range. Show that it gives the right answers on `x`. (You do not have to write a formal test for `quartiles`.)
3. (5) Which points in `x` are outliers, according to Tukey's rule, if any?

4. (20) Write a function, `test.tukey.outlier`, which tests the function `tukey.outlier` against your answer in the previous question. This function should return `TRUE` if `tukey.outlier` works properly; otherwise, it can either return `FALSE`, or an error message, as you prefer. (You can do the next problem first, if you find that easier.)
5. (20) Write `tukey.outlier`, using your `quartiles` function. Show that it passes `test.tukey.outlier`.
6. (5) Which data values should be outliers in `-x`?
7. (5) Which data values should be outliers in `100*x`?
8. (10) Modify `test.tukey.outlier` to include tests for these cases.
9. (5) Show that your `tukey.outlier` function passes the new set of tests, or modify it until it does.
10. (15) According to Tukey's rule, which points in the next vector are outliers? What is the output of your function? If they differ, explain why.

```
y <- c(11.0, 14.0, 3.5, 52.5, 21.5, 12.7, 16.7, 11.7, 10.8, -9.2, 12.3, 13.8)
```