

Example 1: Ginkgo for Memory (3x2 ANOVA)

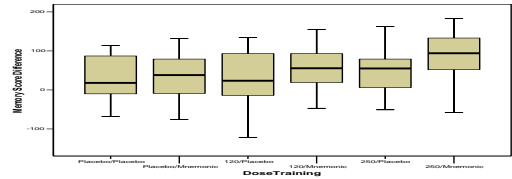
- Test the effects of the herbal medicine Ginkgo biloba (Placebo, 120mg, and 250mg) on memory (treated as categorical because...)
- Also test the effects of "mnemonic training" (no or yes)
- 18 healthy subjects for each factor combination (N = 18 x 6 = 108)
- Memory is tested before the study and after two-months.
- The response variable is the difference (after - before) in the memory test scores [Not violating independent errors.]
- Some data:

Outcome	Dose	Training
9	1	1
-30	1	1
...		
55	3	2
...		

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Example 1, EDA

Memory Score Difference	Dose/Training	Statistic	Std. Error
Placebo/Placebo	Mean	31.00	13.098
	Std. Deviation	55.571	
Placebo/Mnemonic	Mean	34.00	15.525
	Std. Deviation	65.865	
120/Placebo	Mean	29.06	15.908
	Std. Deviation	67.492	
120/Mnemonic	Mean	55.83	12.508
	Std. Deviation	53.065	
250/Placebo	Mean	48.56	14.099
	Std. Deviation	59.818	
250/Mnemonic	Mean	90.44	14.749
	Std. Deviation	62.574	



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Example, cont.

One-way ANOVA for the 6 groups (educational use only!)

	Sum of Squares	Df	Mean Square	F	Sig.
Between Groups	48725.296	5	9745.059	2.623	.028
Within Groups	378948.333	102	3715.180		
Total	427673.630	107			

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Example: Two-way ANOVA with interaction

	Sum of Squares	Df	Mean Square	F	Sig.
Between Groups	48725.296	5	9745.059	2.623	.028
Within Groups	378948.333	102	3715.180		
Total	427673.630	107			

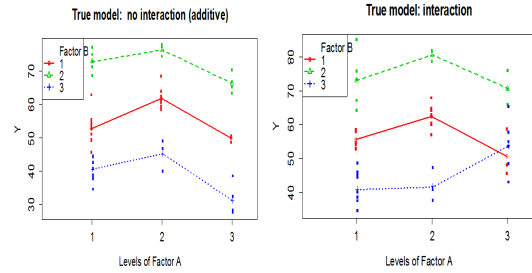
Source	Type III Sum of Squares	df	Mean Square	F	Sig.
Corrected Model	48725.296(a)	5	9745.059	2.623	.028
Intercept	250370.370	1	250370.370	67.391	.000
Dose	26398.741	2	13199.370	3.553	.032
Training	15408.333	1	15408.333	4.147	.044
dose * training	6918.222	2	3459.111	.931	.397
Error	378948.333	102	3715.180		
Total	678044.000	108			
Corrected Total	427673.630	107			

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The meaning of interaction and interaction (profile) plots

- An interaction is always described as being **between two (or more) explanatory variables**, and it indicates that **the effects of changes in level of any one IV on the outcome depends on the level of the other IV**. Also, the interaction is **not** between “levels” of one or both of the factors.
- Interaction (profile) plots
 - Be sure to take into account the sampling error.
 - SPSS “profile” plots show the **current model**, not the truth, i.e. those made with an additive **model** are **always parallel**.
 - “Crossing” is **not** synonymous with interaction!!!

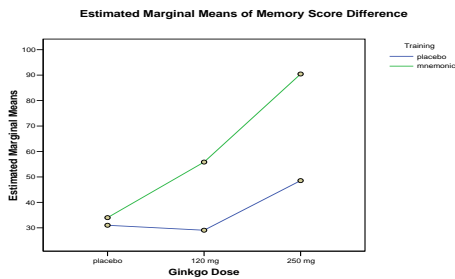
Examples of Interaction Plots



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Example, cont. : SPSS profile plot



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Example: rerun ANOVA without interaction

Source	Type III Sum of Squares	df	Mean Square	F	Sig.
Corrected Model	41807.074(a)	3	13935.691	3.756	.013
Intercept	250370.370	1	250370.370	67.481	.000
dose	26398.741	2	13199.370	3.558	.032
training	15408.333	1	15408.333	4.153	.044
Error	385866.556	104	3710.255		
Total	678044.000	308			
Corrected Total	427673.630	107			

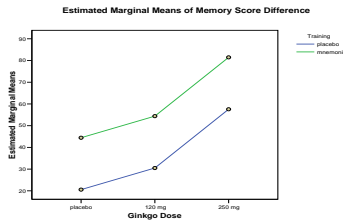
1. Ginkgo Dose					
Dependent Variable: Memory Score Difference					
Ginkgo Dose	Mean	Std. Error	95% Confidence Interval		
			Lower Bound	Upper Bound	
placebo	32.500	10.397	11.882	53.118	
120 mg	40.972	10.397	20.354	61.590	
250 mg	69.500	10.397	48.882	90.118	

2. Training					
Dependent Variable: Memory Score Difference					
Training	Mean	Std. Error	95% Confidence Interval		
			Lower Bound	Upper Bound	
placebo	35.222	8.489	18.388	52.057	
mnemonic	60.093	8.489	43.258	76.927	

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Example, cont.

➤ Additive model profile plot (fitted values):



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Two-way ANOVA interpretation

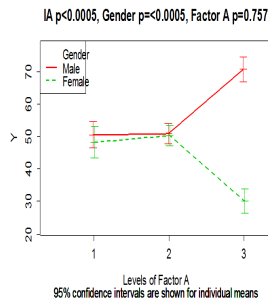
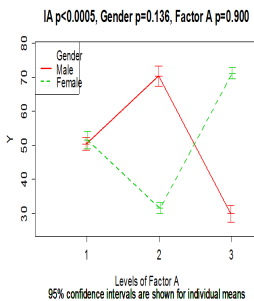
➤ Which analysis should we use to estimate treatment effects?

- If the “no interaction” null hypothesis is rejected, use the “with interaction” model’s ANOVA.
- If the “no interaction” null hypothesis is not rejected (“retained”), use the additive model’s ANOVA. (This may be making a false assumption of no interaction. i.e. a type-2 error.)

➤ If the p-value for **interaction is significant, do not** interpret the “main effects” (dose and training); simply state that both of the explanatory variables affect the outcome in such a way that **the effects of each factor depends on the level of the other factor**. (Contrasts and the profile plots add more interpretability.)

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Two-way ANOVA interpretation



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Two way ANOVA interpretation

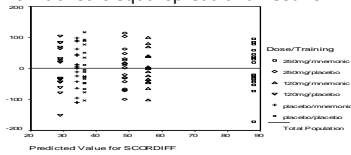
➤ When the **interaction is not statistically significant** interpret each main effect relative to the null hypothesis of equal means across all levels using language like “ignoring” or “averaging over” or “at each level of” the other factor(s).

- If a factor’s p-value is statistically significant (≤ 0.05) and the factor has just **two levels** (like training) look at which of the two levels has the higher mean and make a statement like “mnemonic training improves memory at each dosage” or, better, “mnemonic training improves memory by 24.1 points on average at each dosage”. Adding a 95% CI is even better (1.1 to 48.7 point rise).
- If a factor’s p-value is statistically significant (≤ 0.05) and the factor has **more than two levels** (like dose), then we reject $H_0: \mu_1 = \dots = \mu_k$. Simply state that the (population) mean of the memory score difference for both training types “varies by dose” or “depends on dose” or “differs for at least two doses” for both levels of training. (With contrast testing we can make more detailed conclusions.)

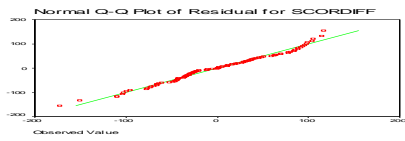
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Model checking: Residual Analysis

- Residual vs. fit checks equal spread and need for interaction



- Quantile normal checks for Normality (robust)



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Three way ANOVA

Subjects: infants

Setup: new toy (one per child) introduced along with distracting sounds

Outcome: attention (amount of time till distraction)

Explanatory variables: Age of child (8,10,12 months)

Size of toy (small vs. large)

Color of toy (red vs. yellow vs. transparent)

Color:size interaction (but no three-way interaction):

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Three way ANOVA, cont.

Three way interaction:

Three way ANOVA, cont.

Results:

Source	Type III Sum of Squares	df	Mean Square	F	Sig.
Corrected Model	25000	8	3125	6.25	0.000
Intercept	4000	1	4000	8.00	0.006
Color	7000	2	3500	7.00	0.002
Size	3000	1	3000	6.00	0.017
Color*Size	5000	2	2500	5.00	0.009
Age	6000	2	3000	6.00	0.004
Error	35000	70	500		
Corrected Total	60000	78	769		

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Summary

- Multi-way between-subjects ANOVA is used for a **quantitative DV, independent errors** and any number of **categorical IVs**.
- With no interactions (additive model) it is assumed that the **effect on the DV of any level change in each specific IV** is a fixed value **unaffected by the level(s) of the other factor(s)**.
- **Interactions** may be present **between any 2 or more IVs** (whole variable, not levels!!!) in their effects on the DV. This gives a **non-parallel plot** and says that for at least some level changes of a specific IV, the effect on the DV **depends on (varies with)** the level(s) of some other IV(s).

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