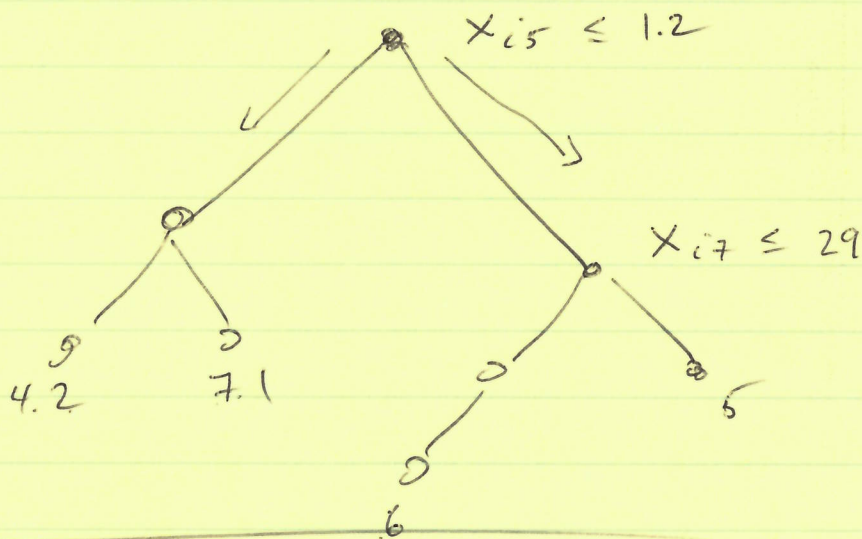


$$x_i = (x_{i1}, \dots, x_{ip})$$



Find tree close to d

instead of ~~update~~

$$u^{(k)} = u^{(k-1)} + t d \quad (\text{usual grad descent})$$

$$\text{ob. } u^{(k)} = u^{(k-1)} + t \cdot \text{Tree}$$

Hence find Tree that's "close to" d .

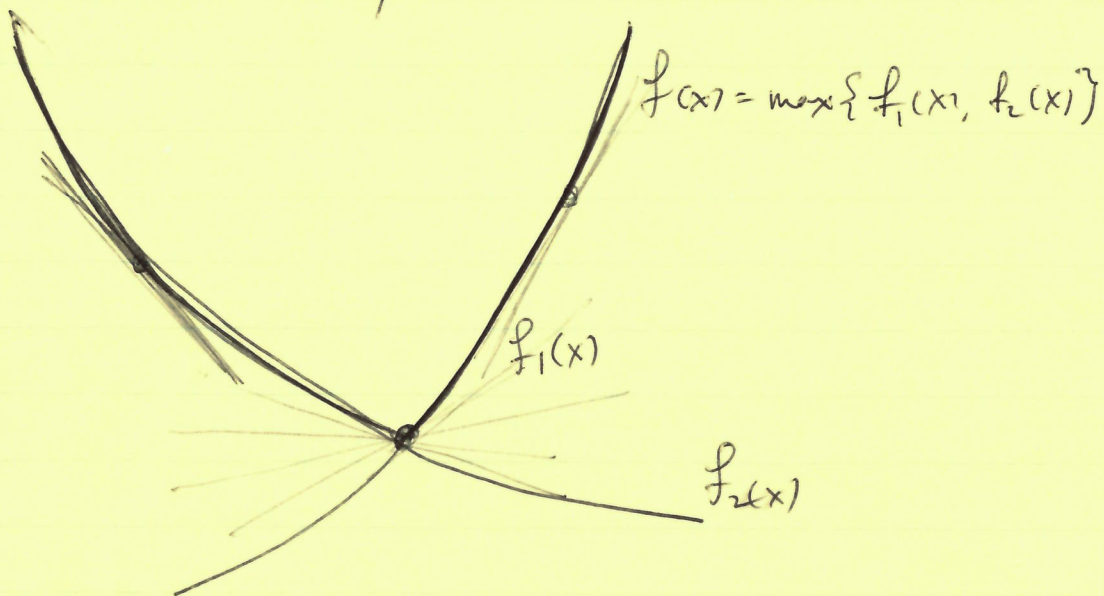
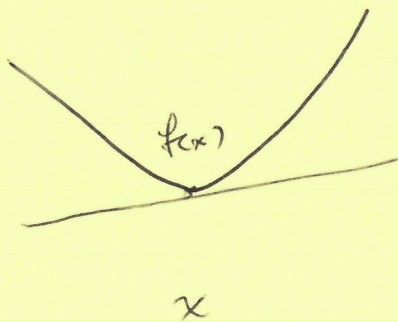
$$\alpha_1 T_1 + \dots + \alpha_r T_r$$

SGD

$$f(\beta) = \|y - X\beta\|_2^2$$

$$= \sum_{i=1}^n \underbrace{(y_i - x_i^T \beta)^2}_{f_i(\beta)}$$

$$g_{ik}^{(k-1)} = \nabla f_{ik}^{(k-1)}(x)$$



$$g = \alpha \nabla f_1(x) + (1-\alpha) \nabla f_2(x)$$

any $\alpha \in [0, 1]$

$$\partial f(x) = \{g: g \text{ is a sub-grad of } f \text{ at } x\}$$

$$* g_1 \in \partial f(x), g_2 \in \partial f(x)$$

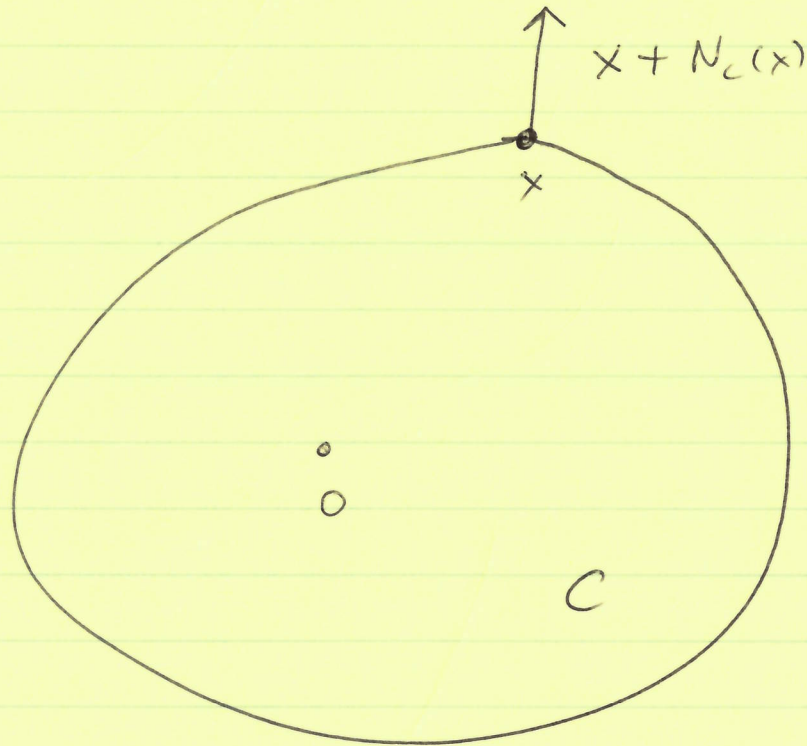
$$(\alpha g_1 + (1-\alpha)g_2)^T (y-x) + f(x) \stackrel{?}{\leq} f(y) \text{ for all } y$$

this is true b/c

$$g_1^T (y-x) + f(x) \leq f(y) \quad \cdot \alpha$$

$$g_2^T (y-x) + f(x) \leq f(y) \quad \cdot (1-\alpha)$$

3



$$f(x) = I_C(x)$$

$$\partial f(x) = \text{conv} \left(\bigcup_{i: f_i(x) = f(x)} \partial f_i(x) \right)$$

$$f(x) = \max \{ f_1(x), f_2(x) \}$$

$\downarrow \quad \downarrow$
 differentiable

$$\text{conv} \left(\{ \nabla f_1(x), \nabla f_2(x) \} \right) = \{ \alpha \nabla f_1(x) + (1-\alpha) \nabla f_2(x) : \alpha \in [0, 1] \}$$

$$\|x\|_p = \max_{z: \|z\|_q \leq 1} z^T x$$

$$\stackrel{u}{f(x)} \quad \quad \quad \stackrel{v}{f_z(x)}$$